

Lux junior 2024

17. Internationales Forum für den lichttechnischen Nachwuchs 6. bis 8. 9. 2024 Dörfeld/Ilm

100 years of $V(\lambda)$ – What's next?

100 Jahre $V(\lambda)$ – Wie geht es weiter?

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Fakultät für Maschinenbau
Fachgebiet Lichttechnik***

Overview

- History: Visual Photometry
- Measuring spectral luminous sensitivity functions
- Spectral luminous efficiency functions since $V(\lambda)$ from 1924
- Cone fundamental based spectral sensitivities
- Impact of introducing cone fundamental based new $V_F(\lambda)$
- Influences still not considered
- Summary

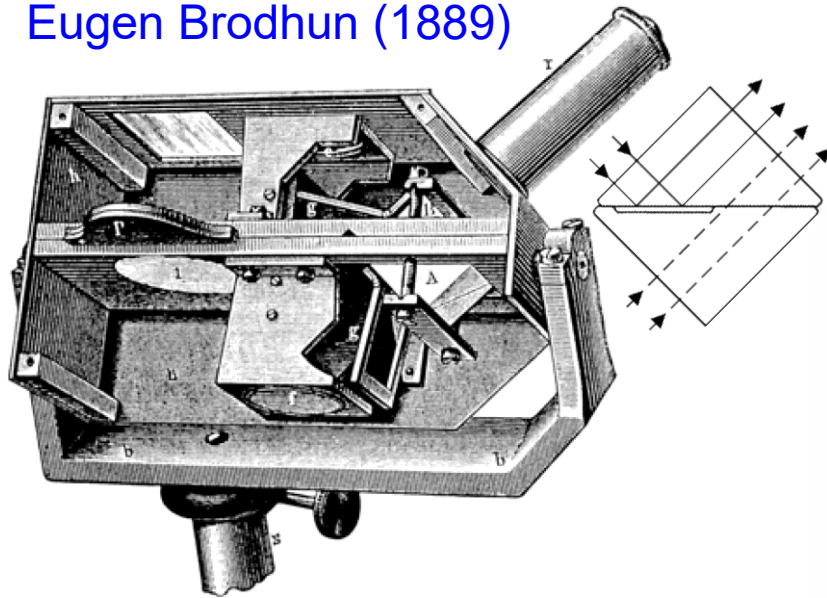
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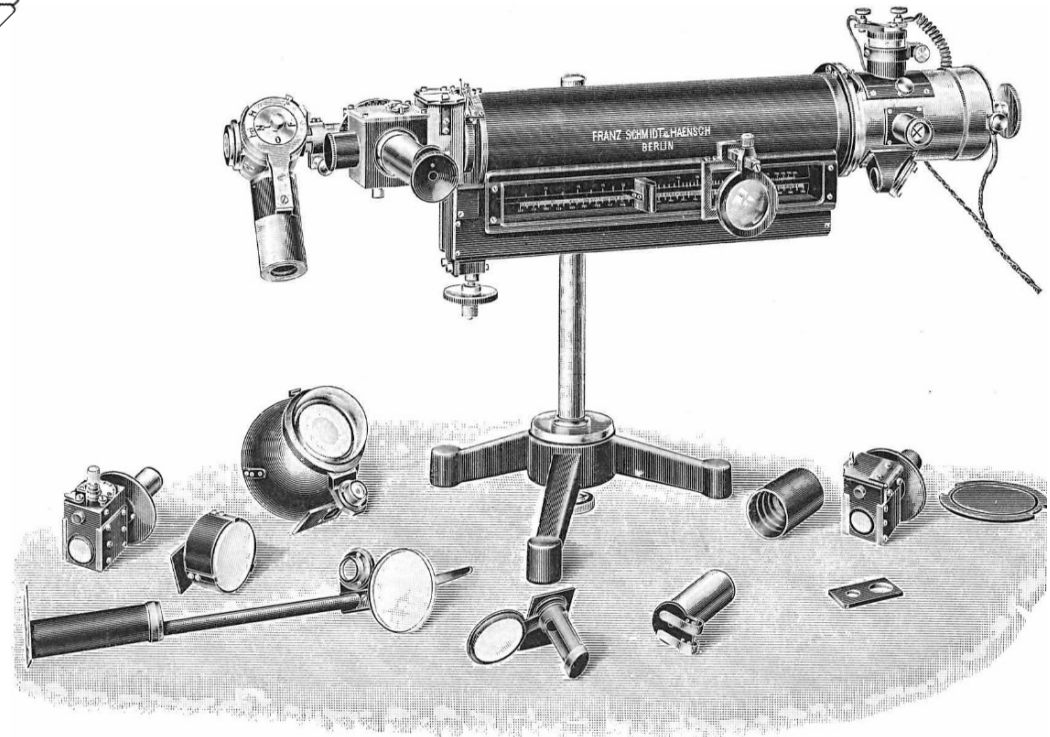
Measurement of brightness

Visual photometry

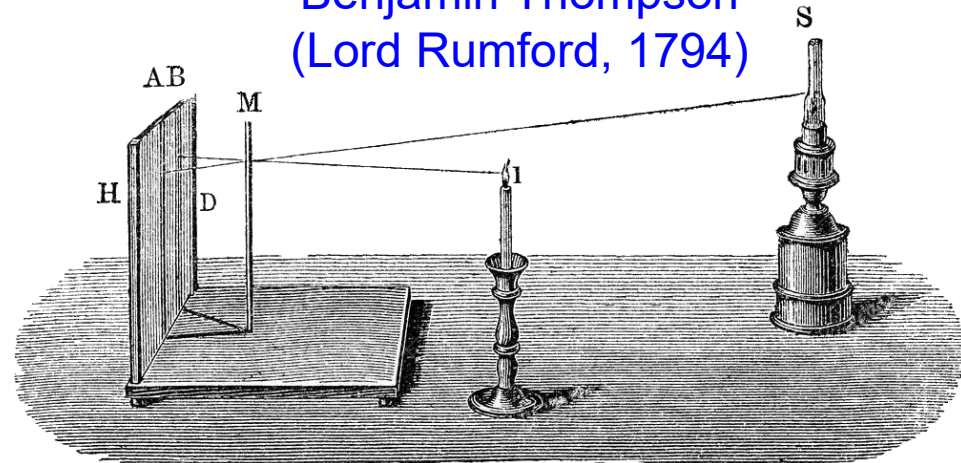
Photometer according to Otto Lummer and Eugen Brodhun (1889)



Universalphotometer Mod. 1
of Schmid & Haensch
with accessories (after 1930)



Photometer according to Benjamin Thompson (Lord Rumford, 1794)



Visual measuring device

Monochromatic Colorimeter

Determination of the concentration of coloured compounds (1854)

Jules Duboscq
(1817-1886)

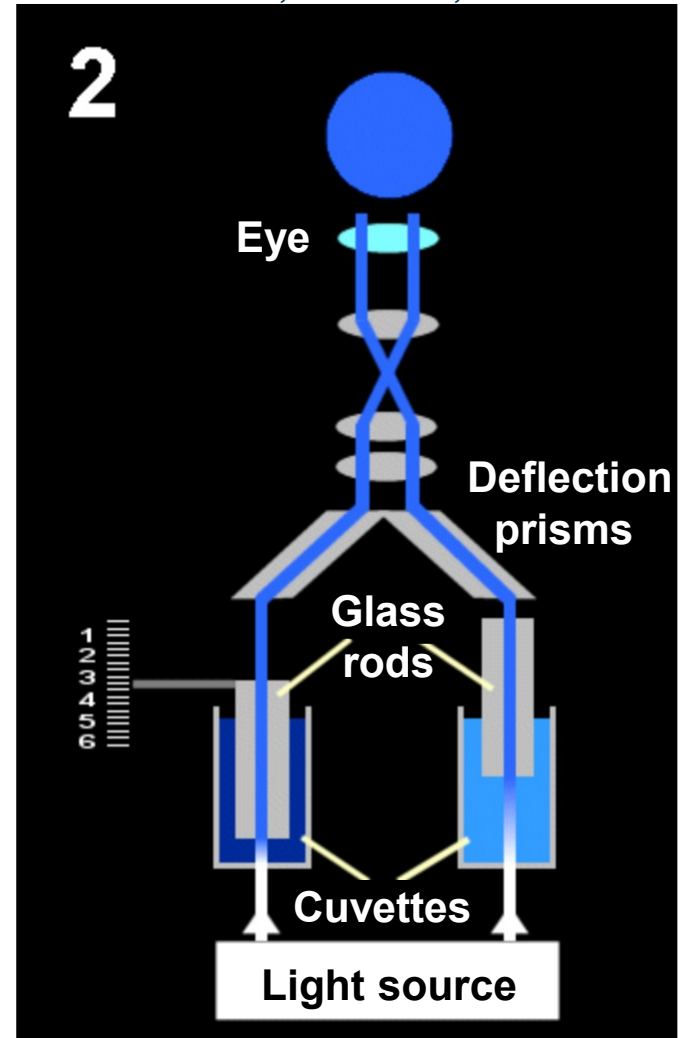


Science Museum Group



1901 – 1914

K. Bauer, W. Hübl, 2002



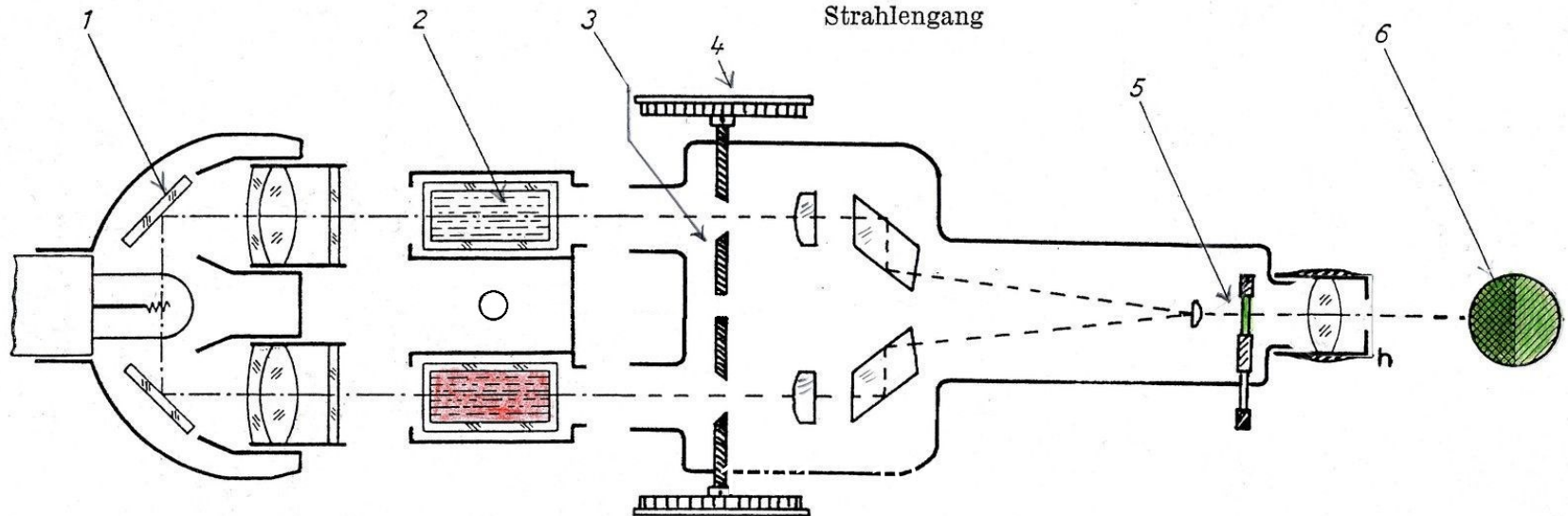
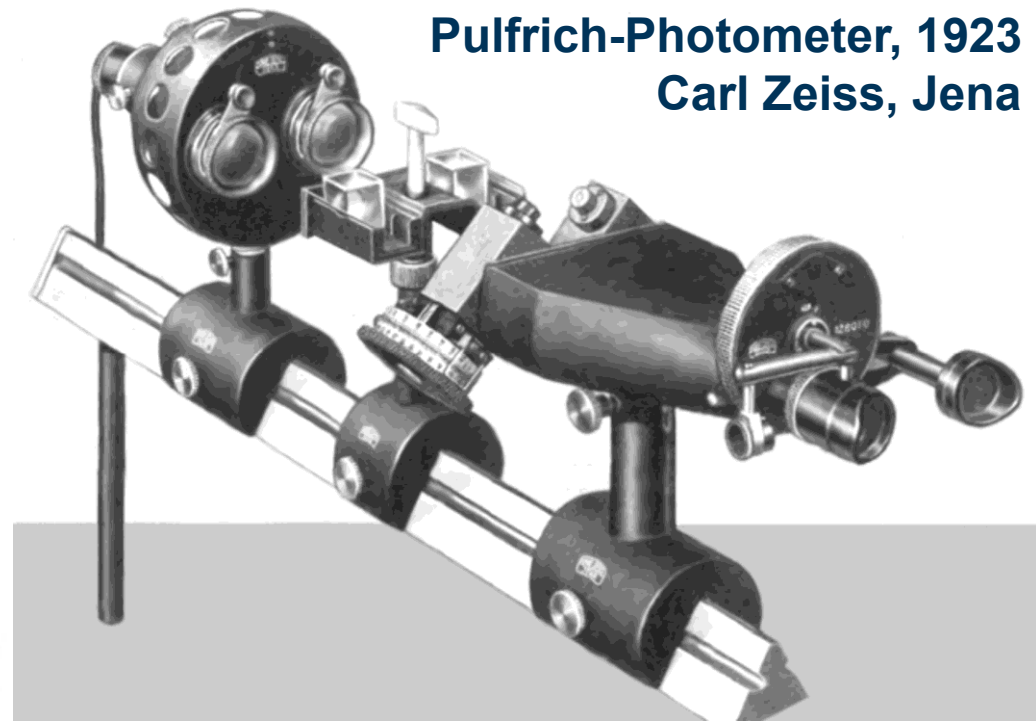
Visual measuring device

Clinical Colorimeter



Carl Pulfrich
(1858-1927)

Pulfrich-Photometer, 1923
Carl Zeiss, Jena



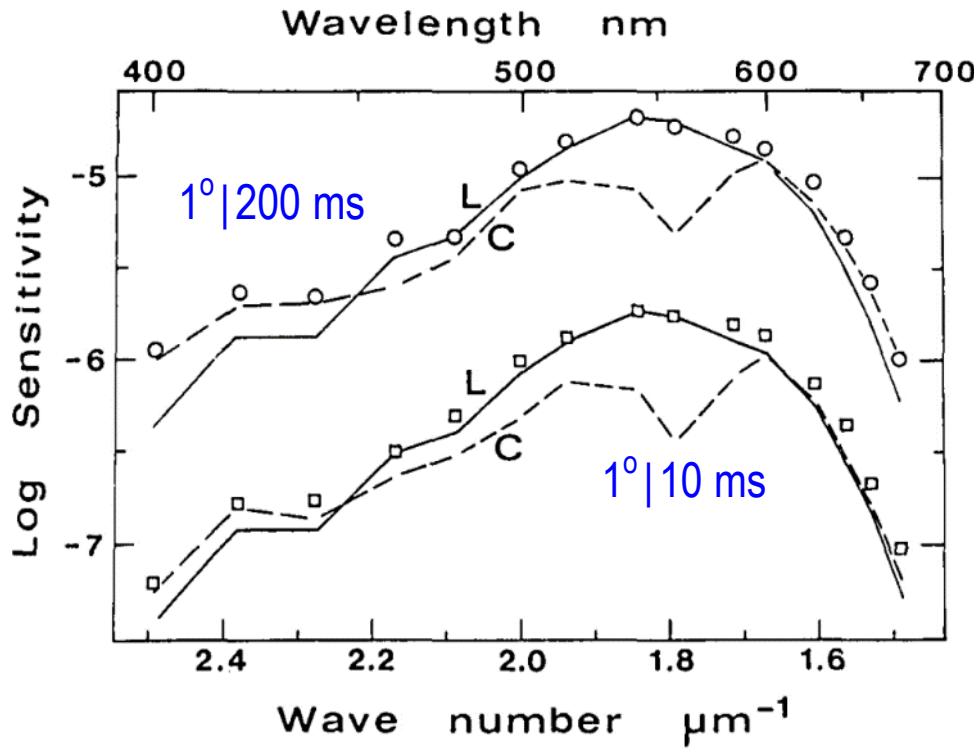
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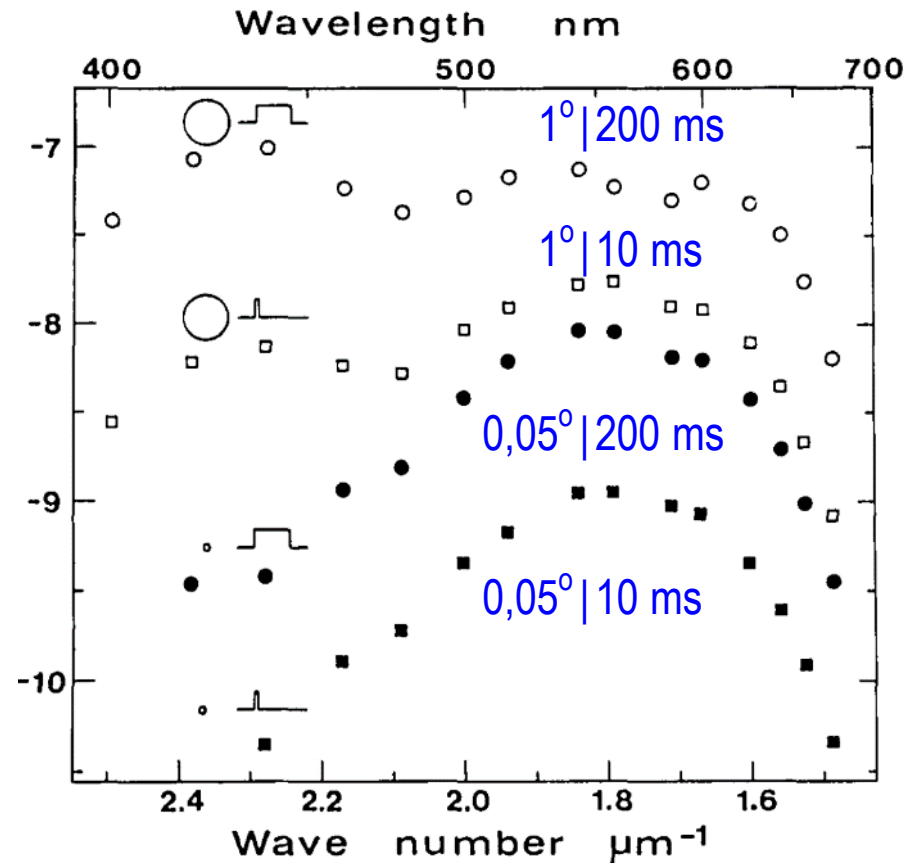
Threshold methods

Absolute threshold on black

Incremental threshold on white



Black background



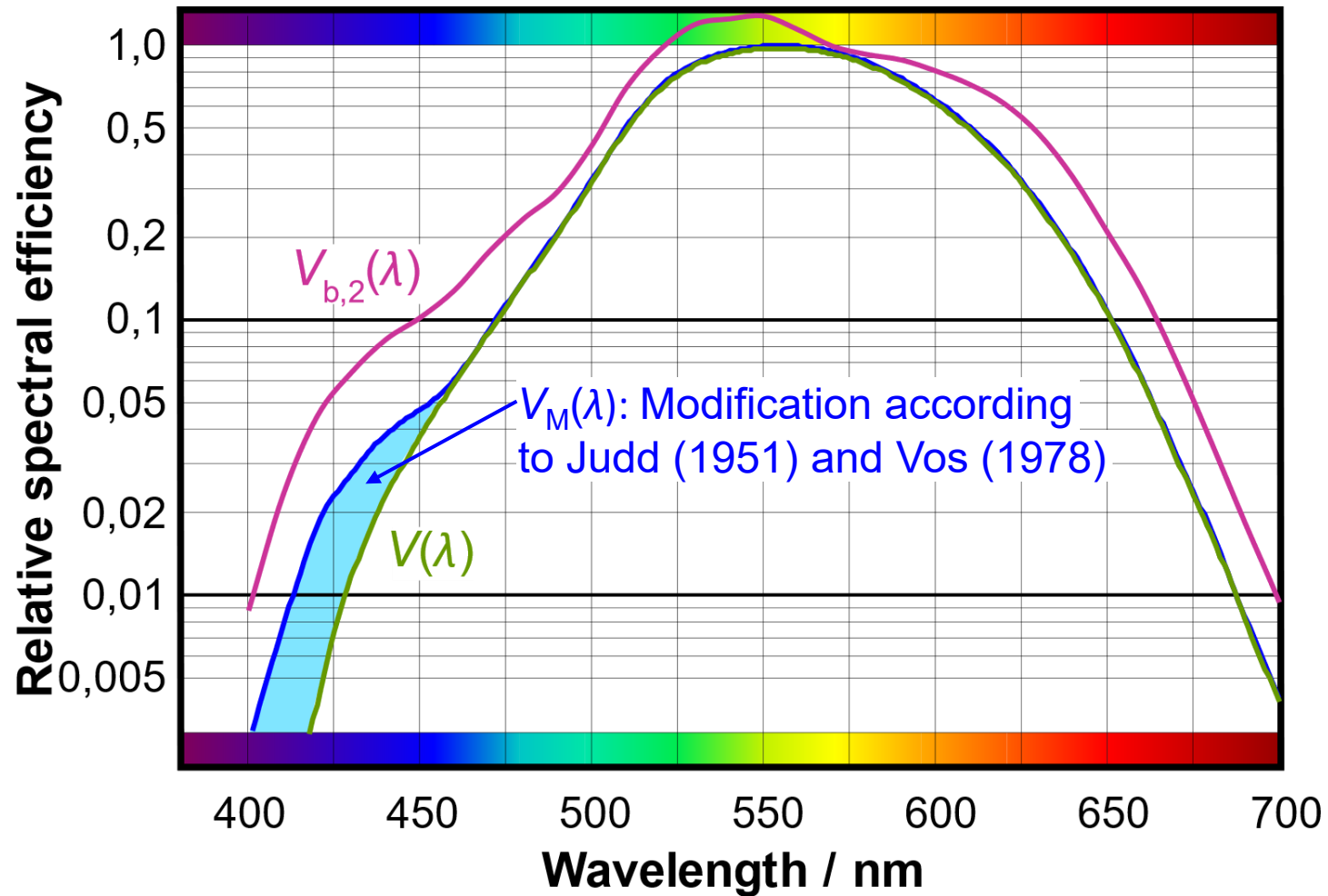
White background
(1000 Troland, size 4° , 3200 K)

P.E. King-Smith, D. Carden, 1976

Direct heterochromatic photometry

$V_{b,2}(\lambda)$: Monochromatic 2° colour stimuli (non-additive)

$V_M(\lambda)$: \approx Monochromatic point source (additive)



CIE Report 75:1988

CIE Report 86:1990

Linear additivity

Abney's law

The total luminance of light composed of several wavelengths is equal to the sum of the luminances of its monochromatic components

Subadditivity: $L_v(\lambda_1 + \lambda_2) < L_v(\lambda_1) + L_v(\lambda_2)$

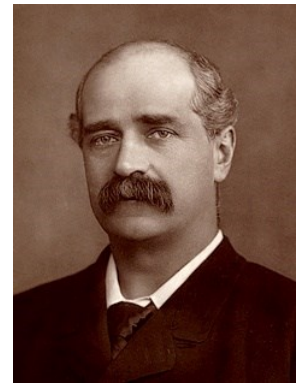
Additivity: $L_v(\lambda_1 + \lambda_2) = L_v(\lambda_1) + L_v(\lambda_2)$

Superadditivity: $L_v(\lambda_1 + \lambda_2) > L_v(\lambda_1) + L_v(\lambda_2)$

Additivity is imperative for a workable system of photometry: $V(\lambda)$ must be additive, regardless of the composition of the spectral radiance $L_{e,\lambda}(\lambda)$. This enables spectral integration with $V(\lambda)$ as a weighting function:

$$L_v = K_m \int_{\lambda} L_{e,\lambda}(\lambda) \cdot V(\lambda) \cdot d\lambda$$

W. Abney et al., 1886
W. Abney, 1913



Sir William Abney
(1843 – 1920)

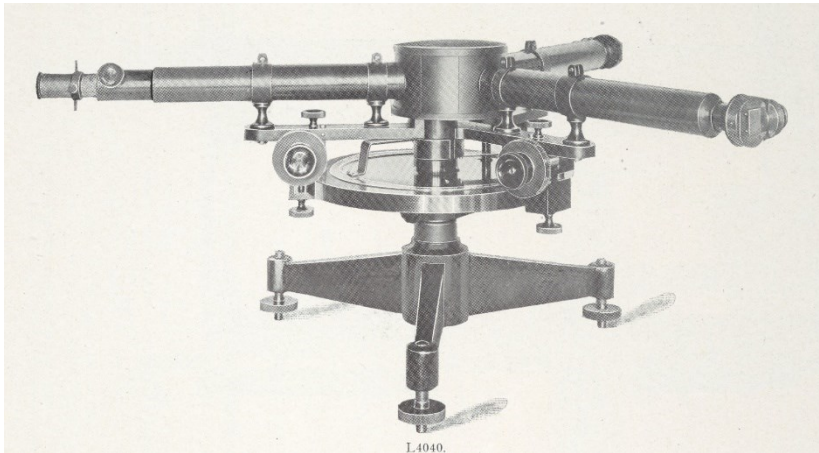
Direct heterochromatic photometry



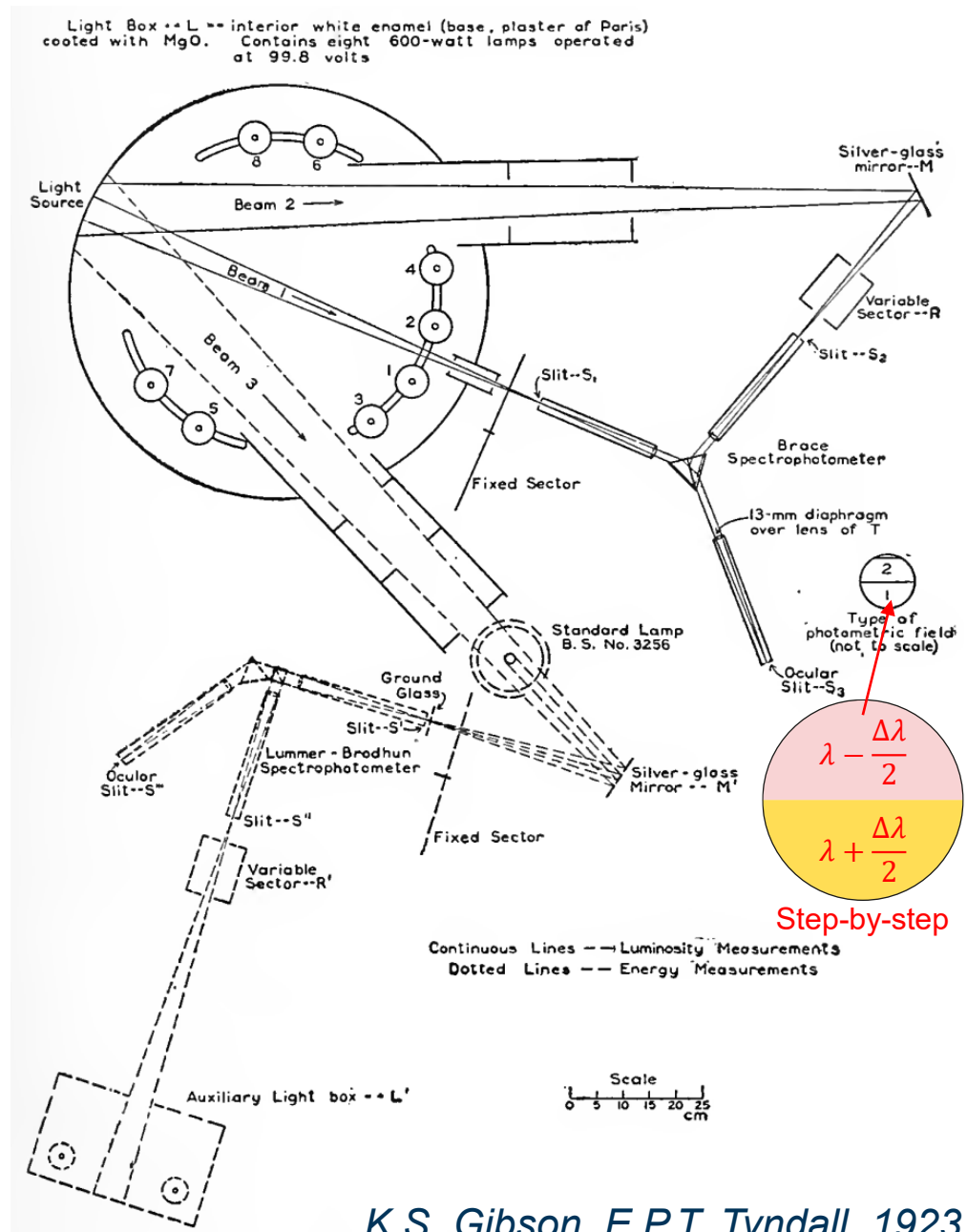
Kasson S. Gibson
(1890 – 1979)



Edward P. T. Tyndall
(1893 - 1979)



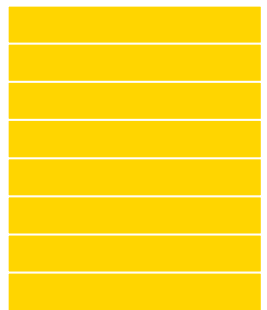
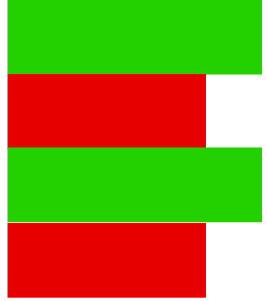
Brace Spectrophotometer



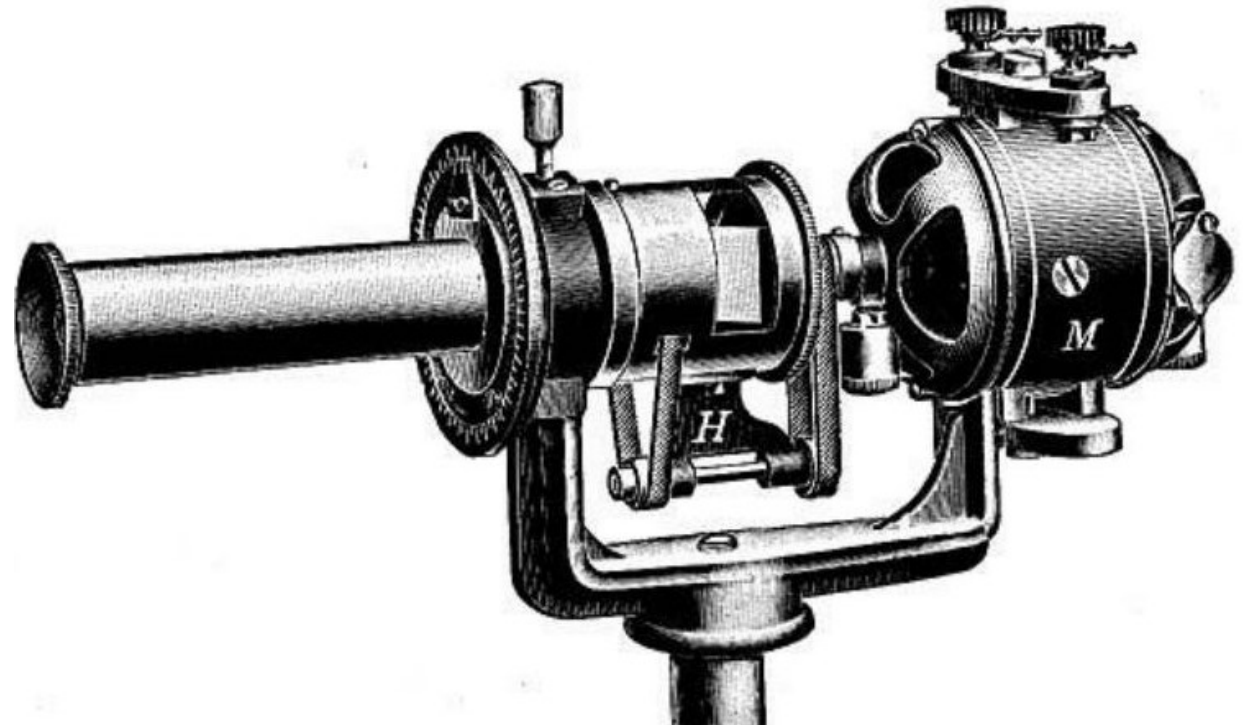
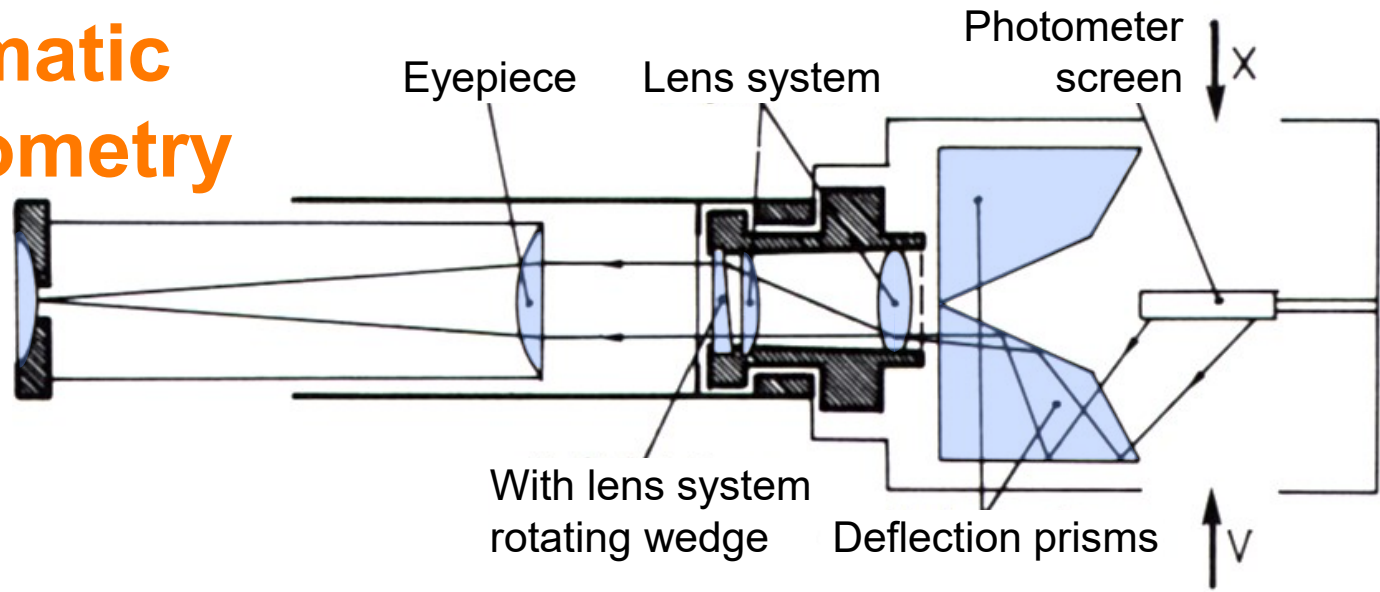
K.S. Gibson, E.P.T. Tyndall, 1923

Heterochromatic flicker photometry

Intensity



Time



Measuring spectral-sensitivity functions

Overview

P. Lennie et al., 1993

Method	Stimulus	Function form	Additivity
Using temporal or spatial alternation			
Heterochromatic flicker photometry (HFP)	low luminance	$V(\lambda)$ -like	Yes
	high luminance	$V(\lambda)$ -like	No
Grating visual acuity		$V(\lambda)$ -like	Yes
Motion minimisation		$V(\lambda)$ -like	Yes
Direct heterochromatic photometry			
Brightness matching	small	$V(\lambda)$ -like	Yes
	large	Broader	No
Step by step equality of brightness		$V(\lambda)$ -like	Yes
Minimally distinct border (MDB)		$V(\lambda)$ -like	Yes
Checkerboard patterns	3' juxtaposed elements	$V(\lambda)$ -like	Yes
	3' separated elements	$V(\lambda)$ -like	No
Threshold methods			
Absolute threshold	small, brief	$V(\lambda)$ -like	Yes
	large, long	Notch @ 570 nm	No
Increment threshold on white background	small, brief	$V(\lambda)$ -like	≈ Yes
	large, long	3 broad peaks	No
Radiance for critical flicker fusion (CFF)	low photopic luminance	$V(\lambda)$ -like	
Landolt C visual acuity		$V(\lambda)$ -like	Yes
Increment grating detection	1 Troland	$V(\lambda)$ -like	Yes
	1000 Troland	Broader	No @ low c/\circ
Speeded response			
Criterion reaction time		$V(\lambda)$ -like	

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V(λ) data compilation

Step-by-step method

Flicker method

K.S. Gibson, E.P.T. Tyndall, 1923

<https://vlambda.machtgluecklich.shop/>

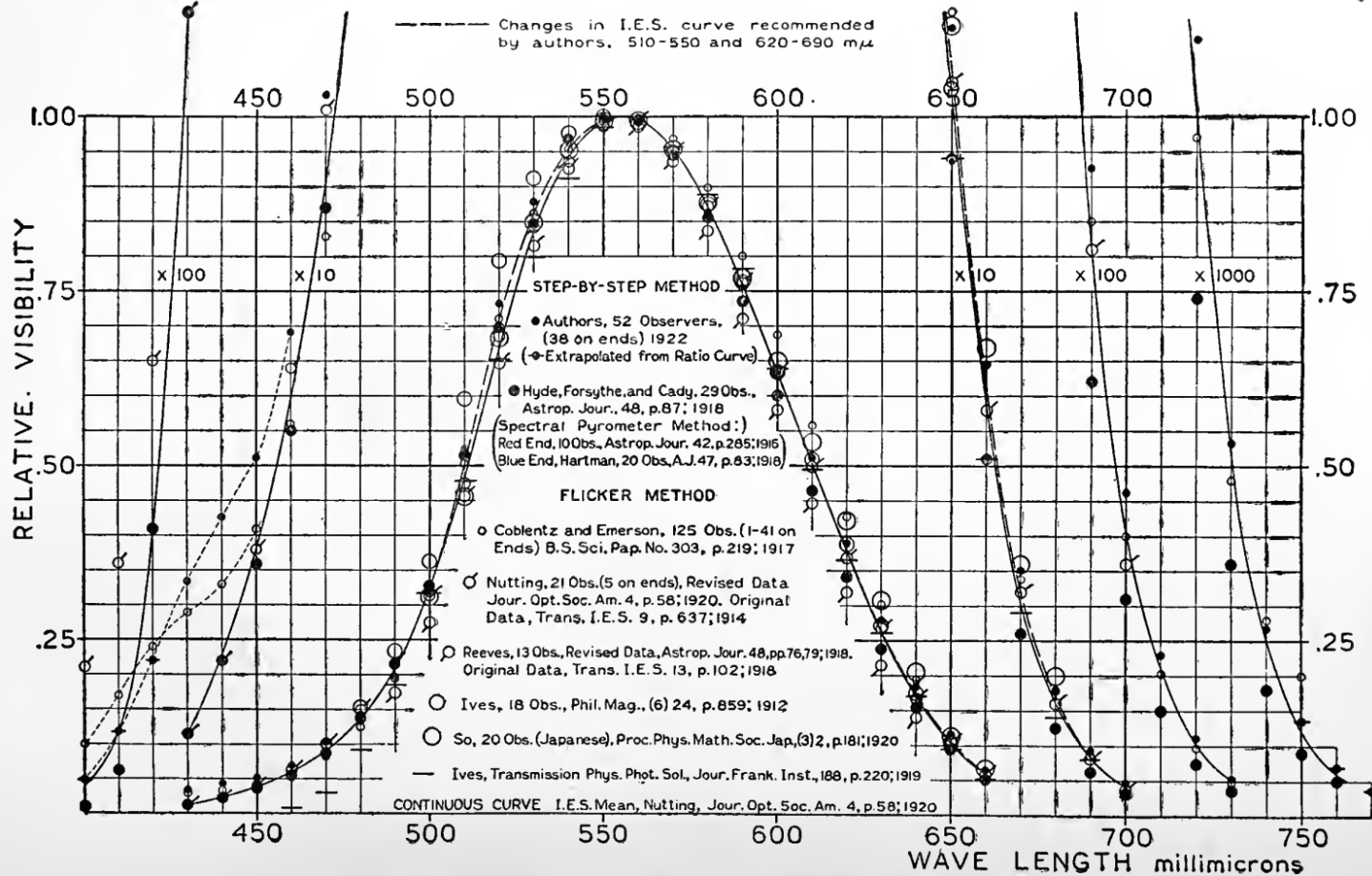
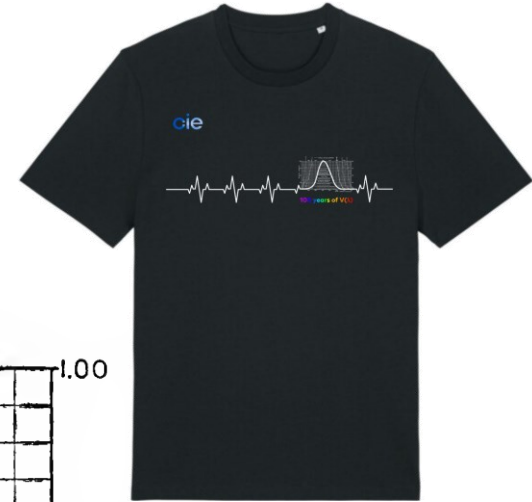
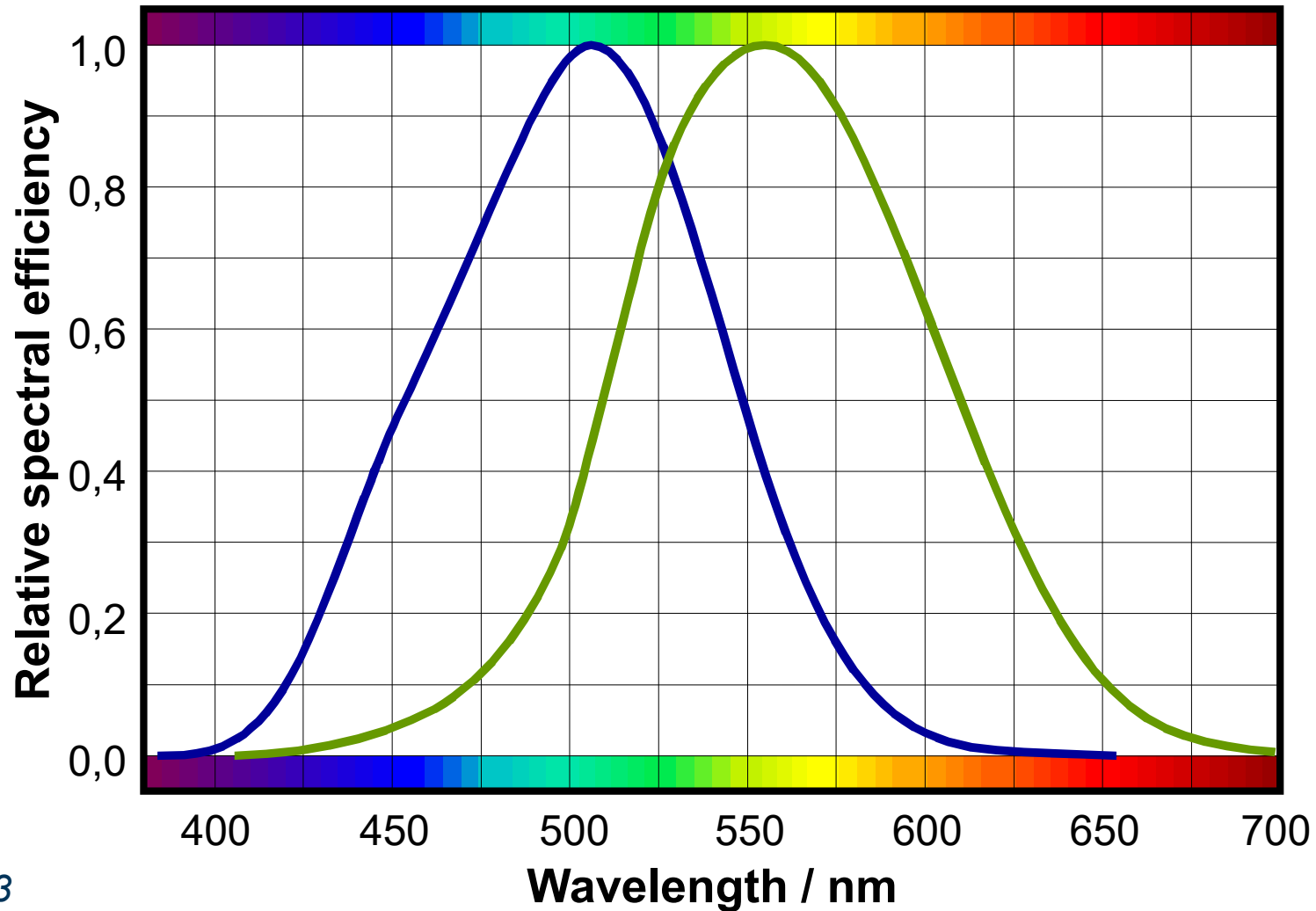


FIG. 19.—Compilation of visibility data. See Table 3 and Figure 21.

Spectral luminous efficiency functions

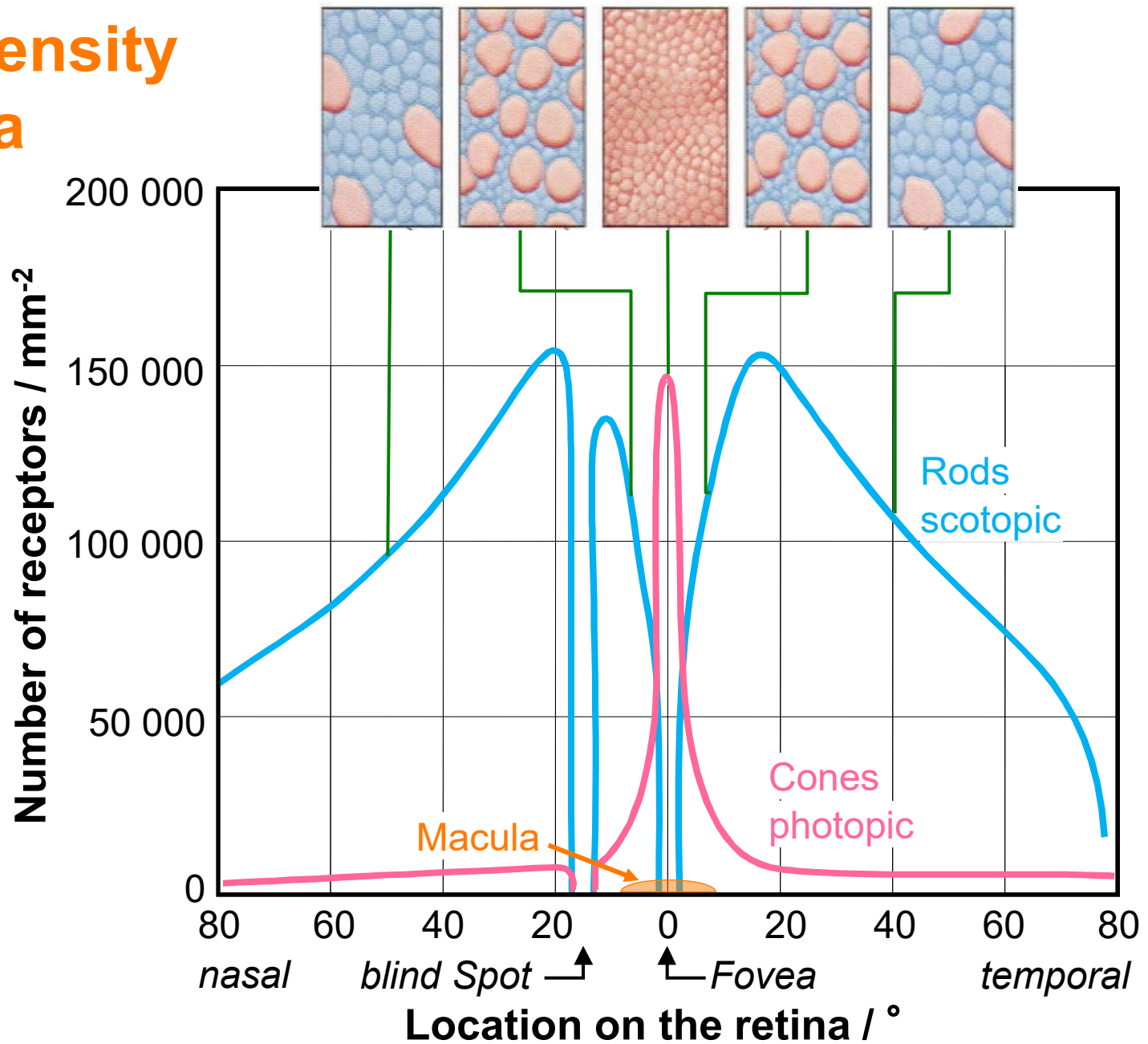
$V'(\lambda)$ scotopic (night vision)
from 1951, field outside macula

$V(\lambda)$ photopic (day vision)
from 1924, field size of 2°



ISO/CIE 23539:2023

Receptor density of the retina



G. Osterberg, 1935

Spectral luminosities introduced by the CIE

Overview

Symbol	Introductory year	Application context	Current reference
$V(\lambda)$ = $\bar{y}(\lambda)$	1924 1931	Luminance region, field size (remark) photopic, 2°	ISO/CIE 23539:2023 ISO/CIE 11664-1:2019
$V'(\lambda)$	1951	scotopic, 20° + 1° [8° above fovea]	ISO/CIE 23539:2023
$\bar{y}_{10}(\lambda)$ = $V_{10}(\lambda)$	1964 2005	photopic, 10°	ISO/CIE 11664-1:2019 ISO/CIE 23539:2023
$V_{b,2}(\lambda)$	1988	photopic, 2° (monochromatic source)	CIE 075-1988
$V_{b,10}(\lambda)$	1988	photopic, 10° (monochromatic source)	CIE 075-1988
$V_M(\lambda)$	1990	photopic, 2° (Judd-Vos correction)	CIE 086-1990
$V_a(\lambda)$	2011	photopic, 2° (age dependent)	CIE 196:2011
$V_F(\lambda)$	2015	photopic, 2° (cone-fundamental)	CIE 170-2:2015
$V_{F,10}(\lambda)$	2015	photopic, 10° (cone-fundamental)	CIE 170-2:2015
$V_{mes;m}(\lambda)$	2023	mesopic, ??° (luminance dependent)	ISO/CIE 23539:2023

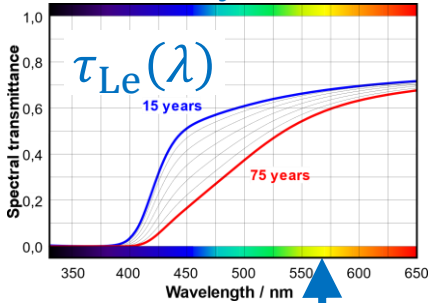
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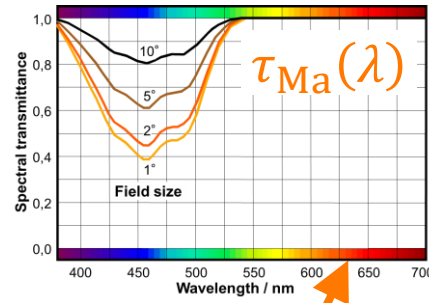
Stages from spectrum to cone responses

Spectral transmissions and absorptions

Spectral transmittance of the eye lens



Spectral transmittance of the macula



Cone fundamentals

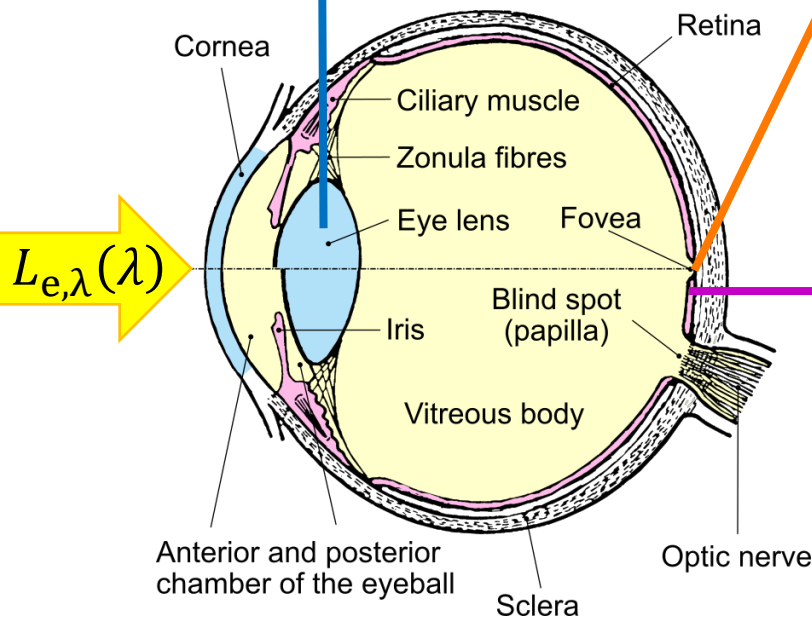
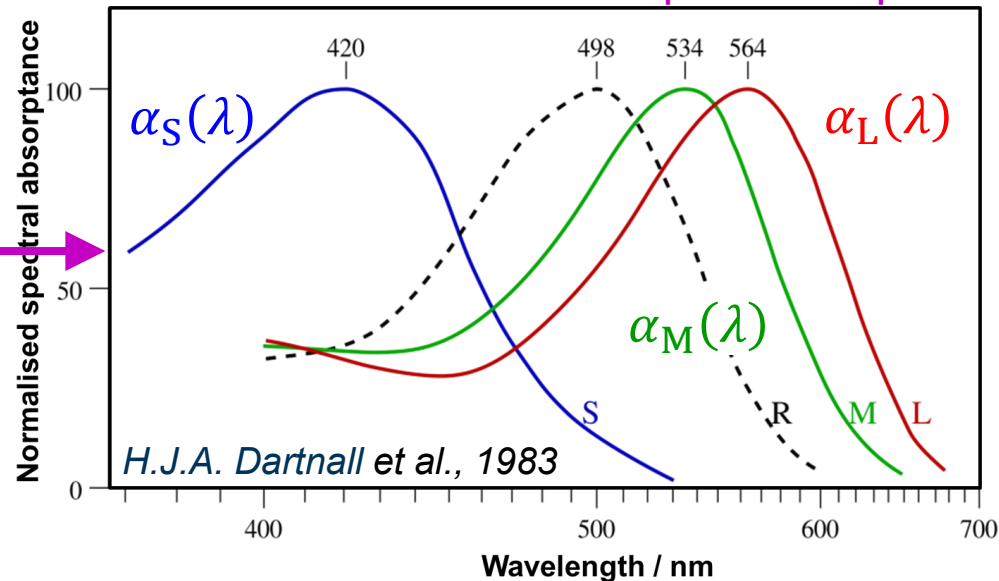
“Sehzapfen-Grundfunktionen”

$$\bar{l}(\lambda) = \tau_{Le}(\lambda) \cdot \tau_{Ma}(\lambda) \cdot \alpha_L(\lambda)$$

$$\bar{m}(\lambda) = \tau_{Le}(\lambda) \cdot \tau_{Ma}(\lambda) \cdot \alpha_M(\lambda)$$

$$\bar{s}(\lambda) = \tau_{Le}(\lambda) \cdot \tau_{Ma}(\lambda) \cdot \alpha_S(\lambda)$$

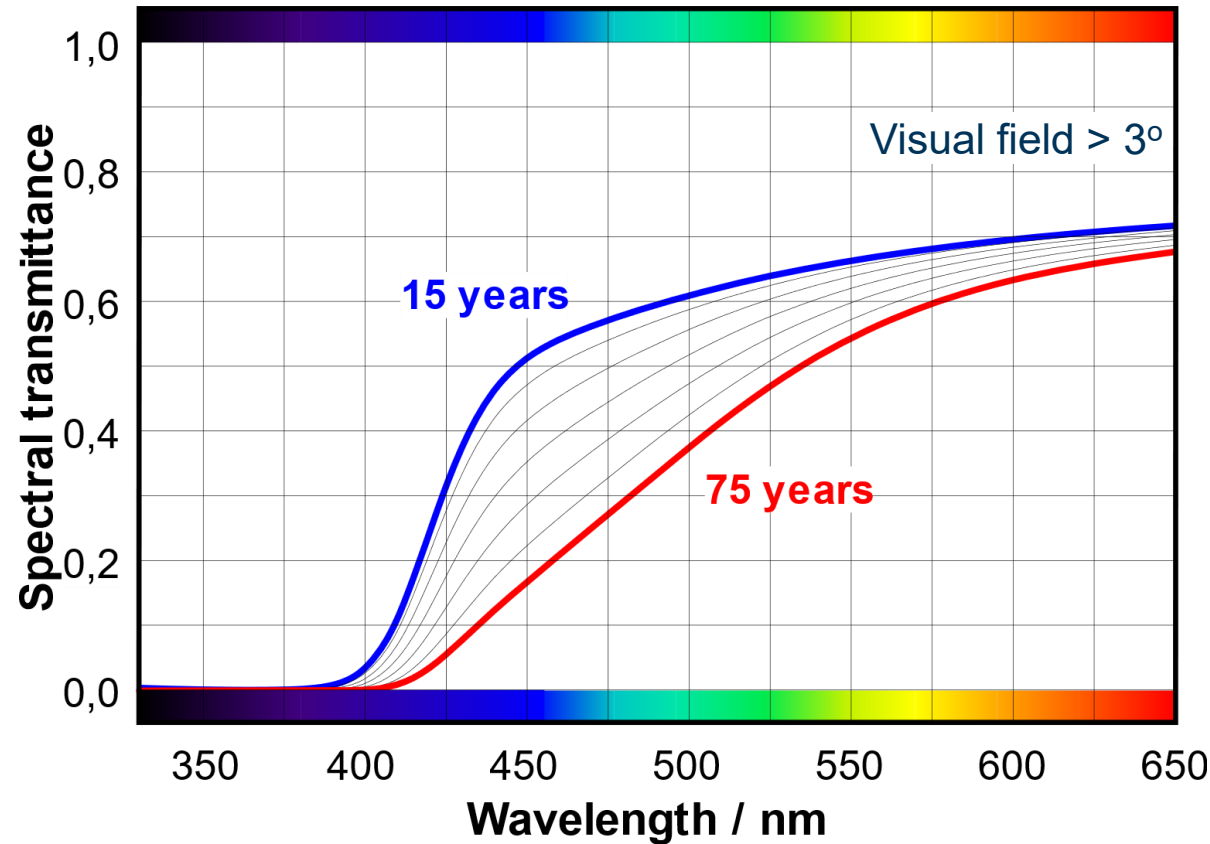
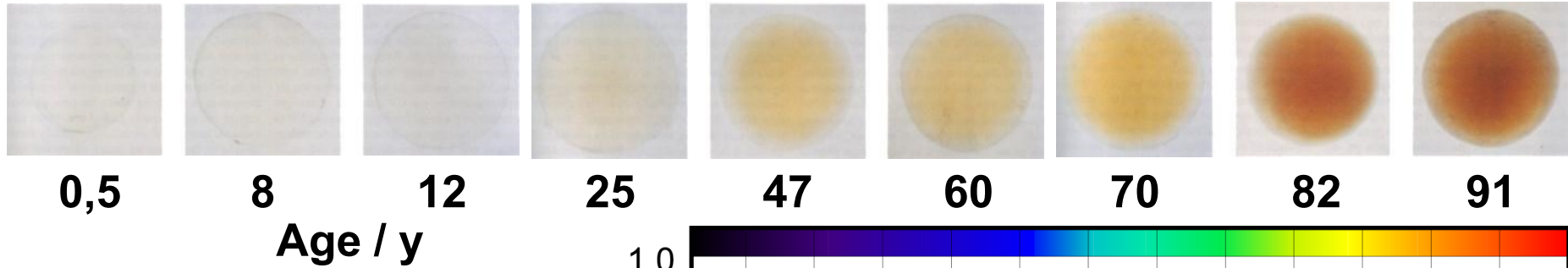
Spectral absorptance of the photoreceptors



Eye lens transmittance

Age dependency

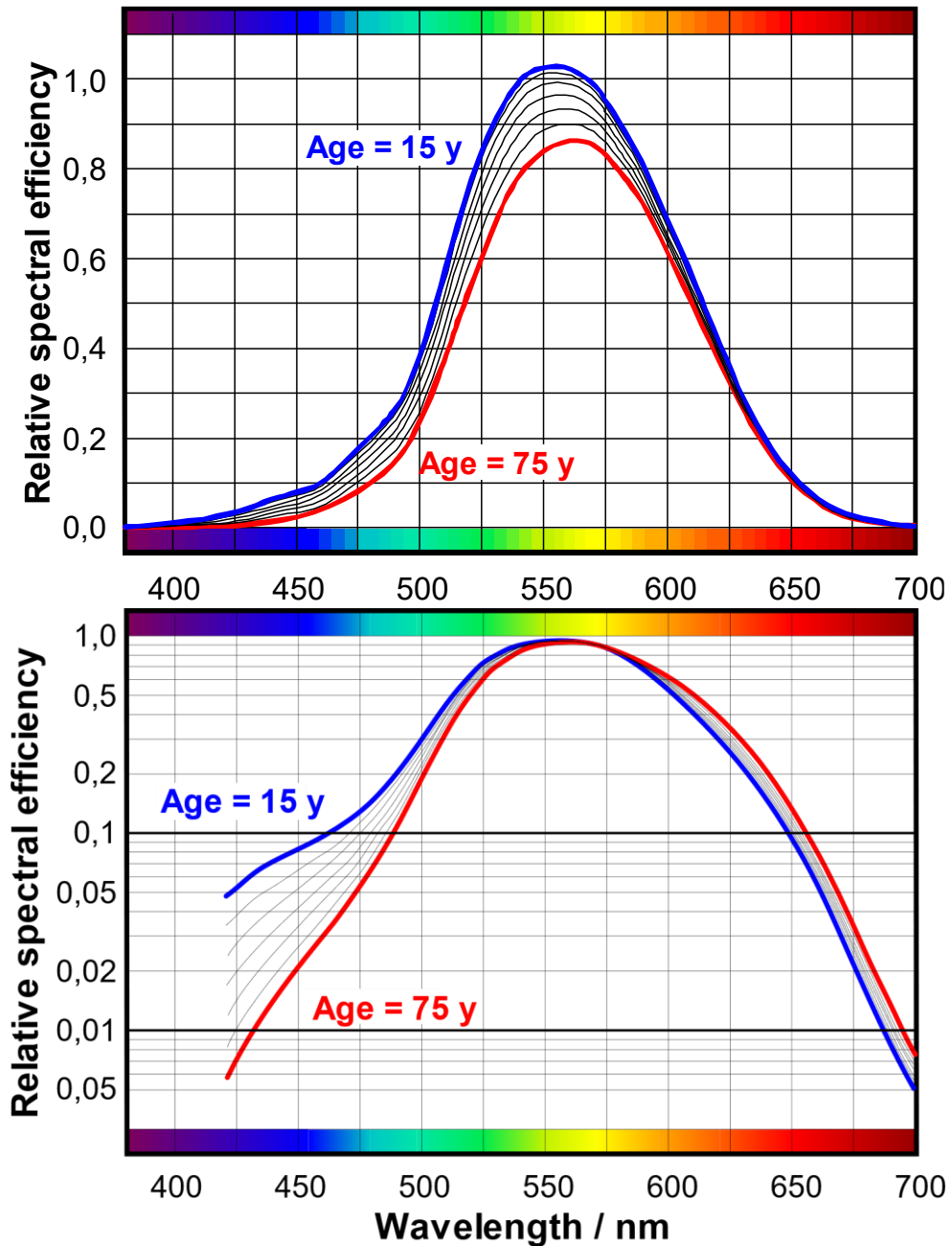
S. Lerman, 1980



van de Kraats et al., 2007

Spectral luminous efficiency $V_a(\lambda)$

Age-dependent, photopic, visual field 2°



CIE 196:2011

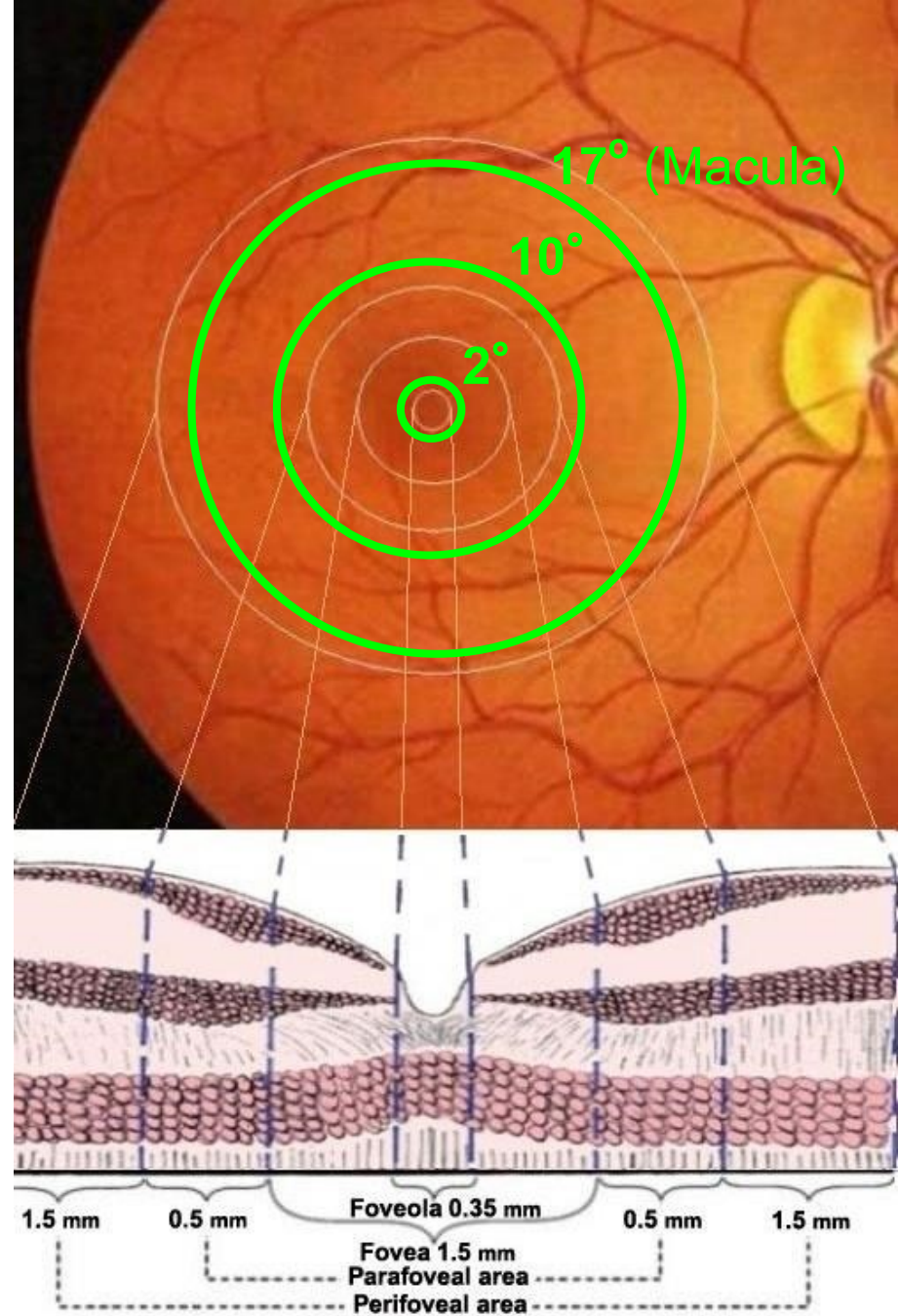
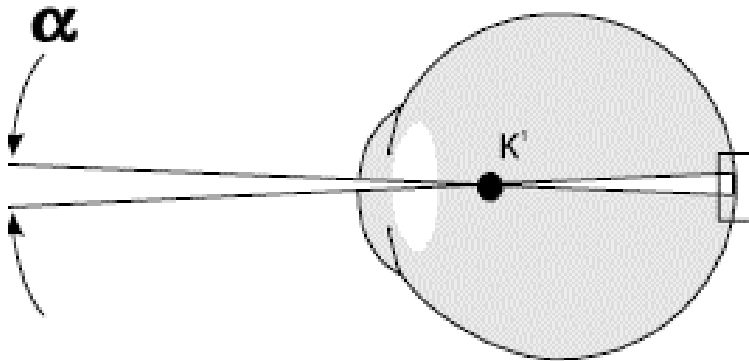
K. Sagawa, Y. Takahashi, 2001

Macula (yellow spot)

Foveal anatomy of the retina

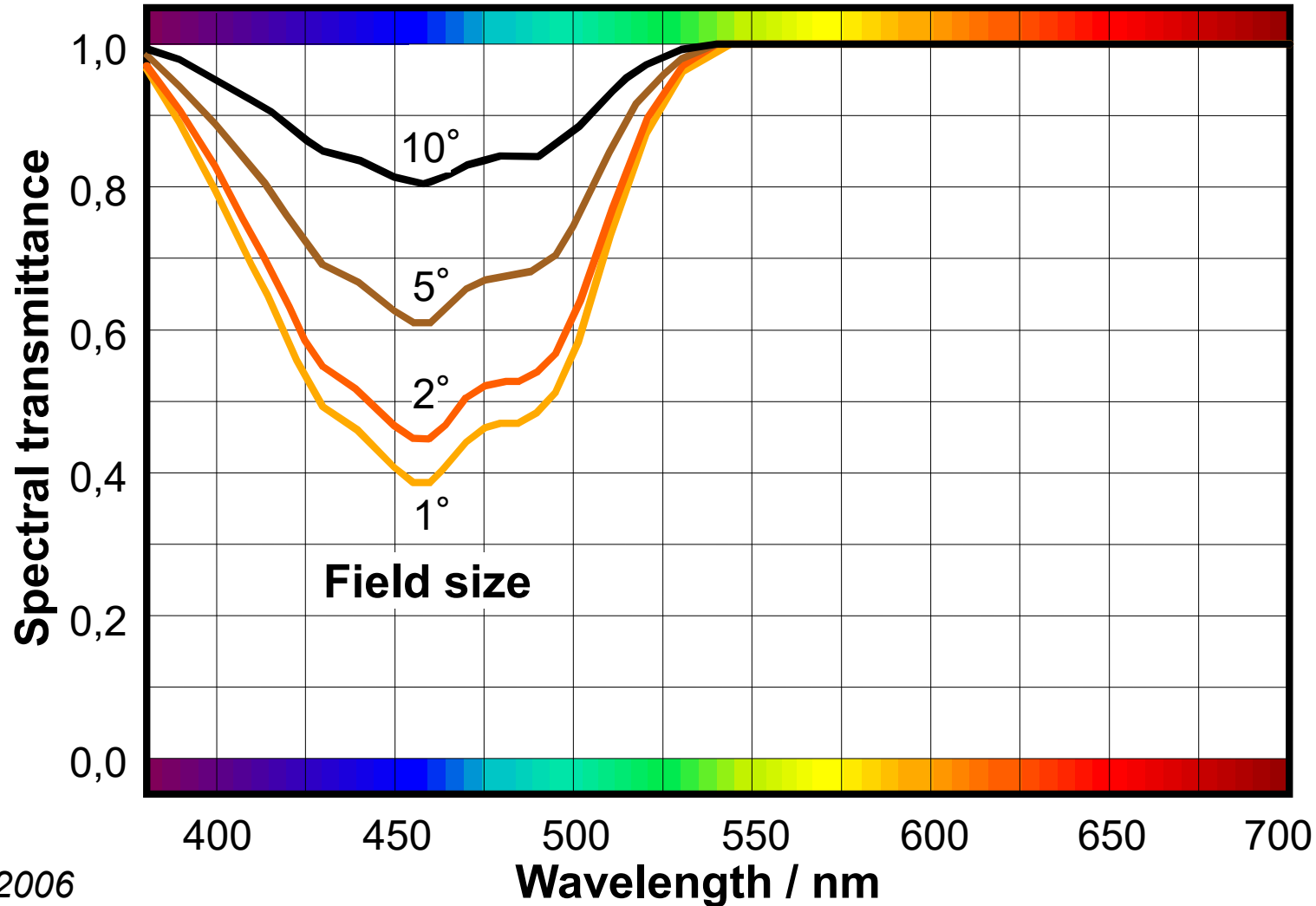
Visual angle α

- e.g. 2° (with 0,6 mm diameter)
- 10° (with 3,0 mm diameter)
- 17° (with 5,0 mm diameter)



Macula (yellow spot)

Transmittance and influence of the field size

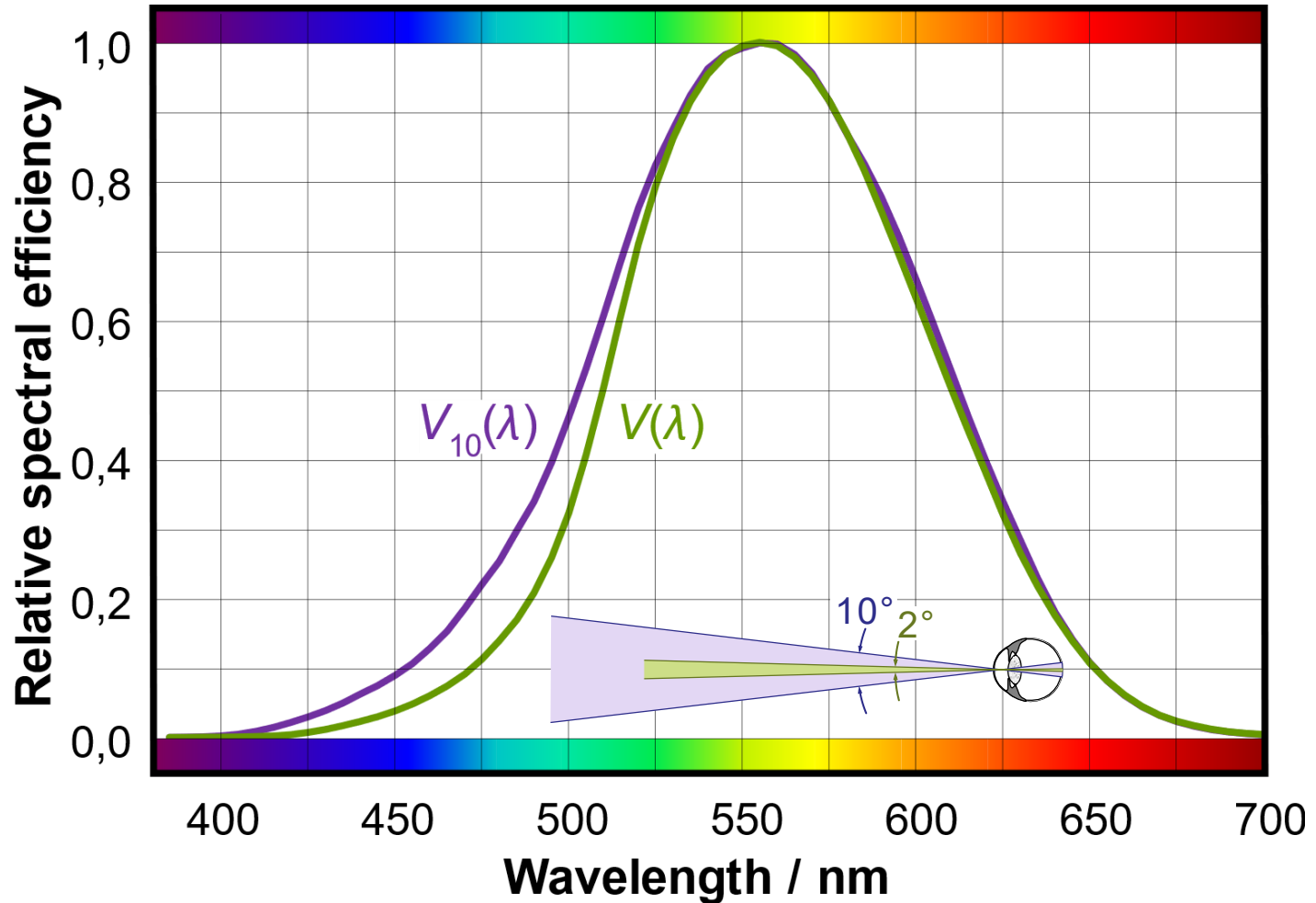


CIE Report 170-1:2006

Spectral luminous efficiency function

$V_{10}(\lambda)$ photopic vision
from 2005, for a field size of 10°

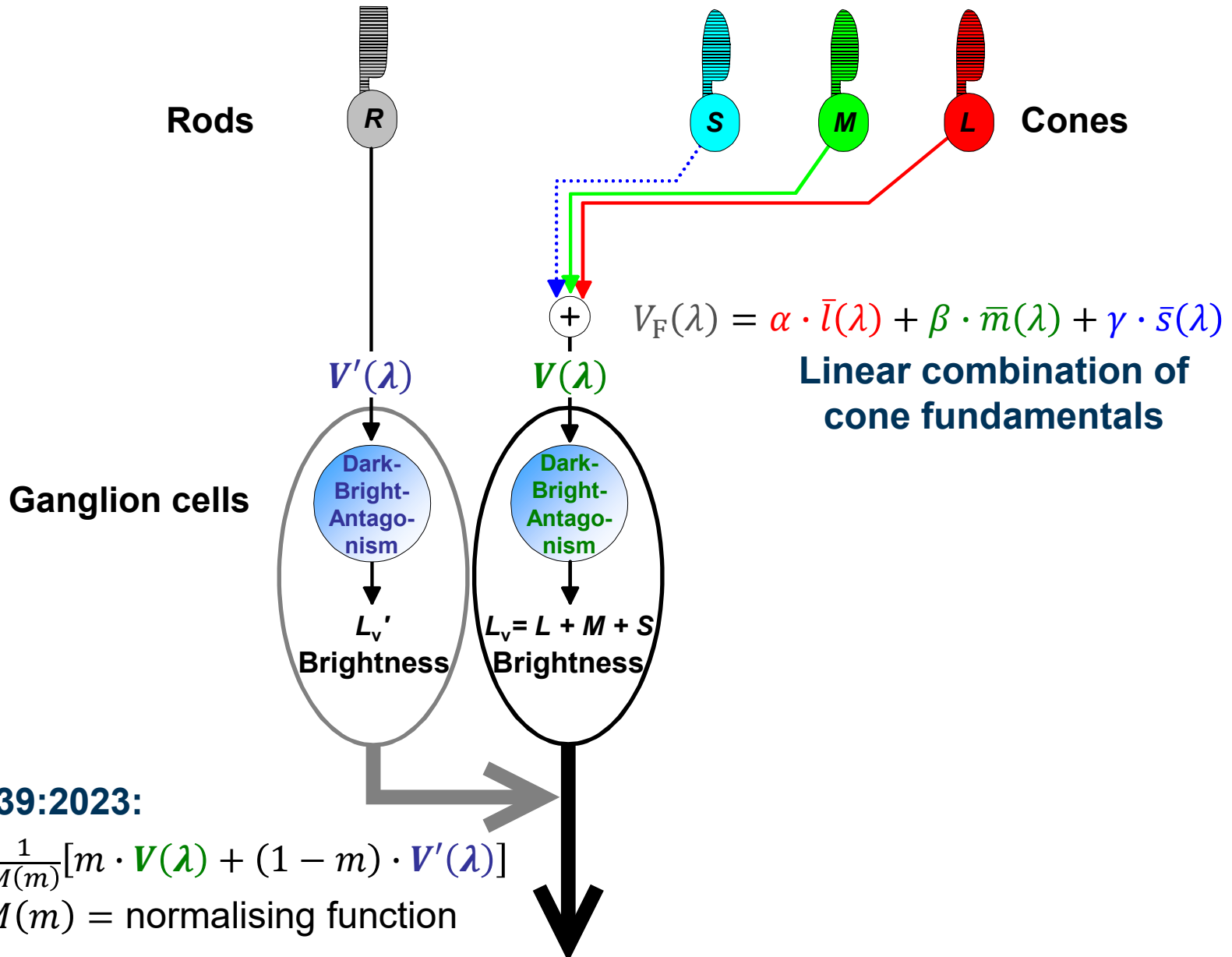
$V(\lambda)$ photopic vision
from 1924, for a field size of 2°



ISO/CIE 23539:2023

Physiological basics of photometry

Photopic
Mesopic
Scotopic



ISO/CIE 23539:2023:

$$V_{\text{mes};m}(\lambda) = \frac{1}{M(m)} [m \cdot V(\lambda) + (1 - m) \cdot V'(\lambda)]$$

$0 \leq m \leq 1$; $M(m)$ = normalising function

M- and L-Cone fundamentals

A. Stockman, L.T. Sharpe, 2000

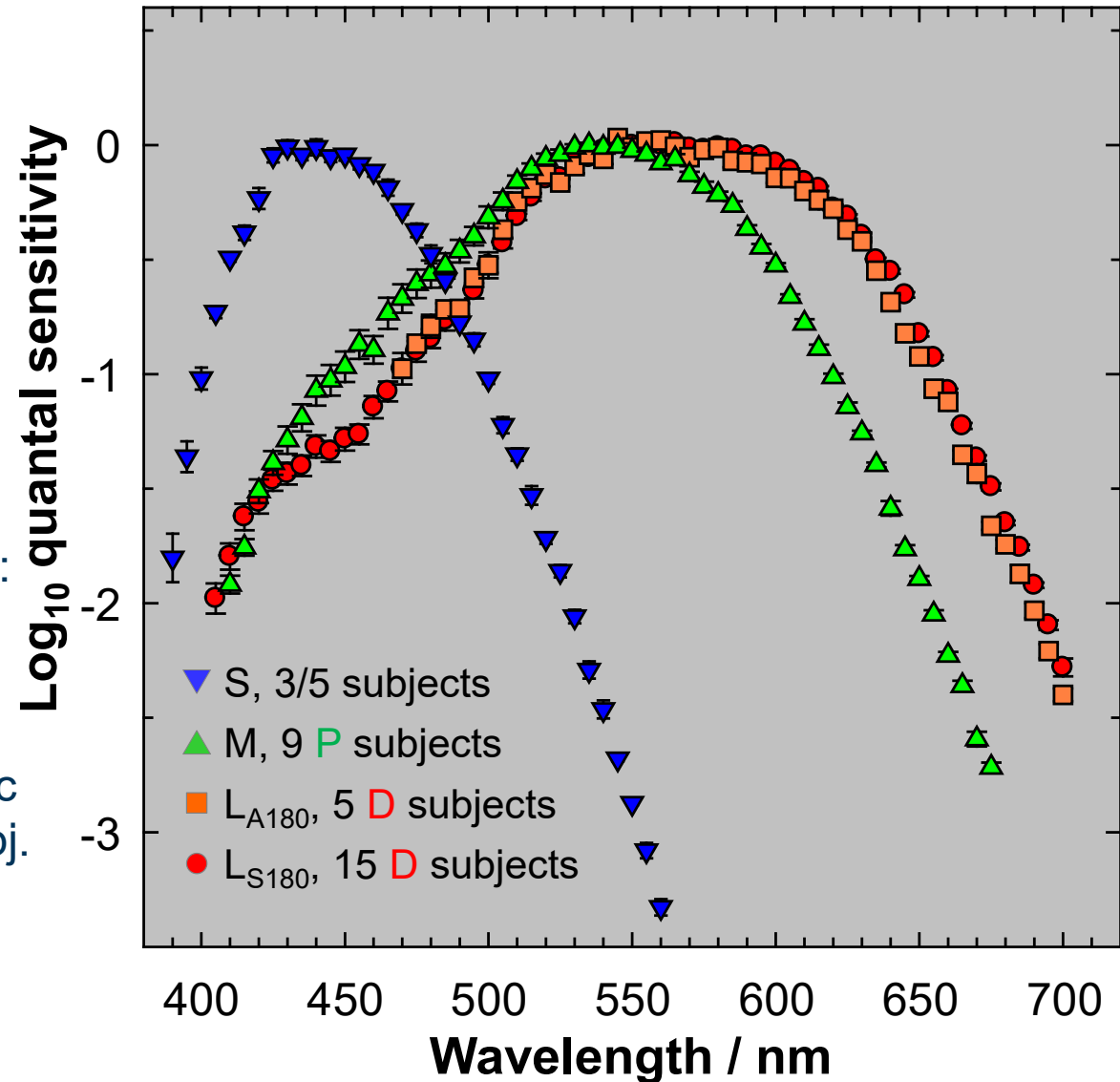
Measurements in observers

▼ → A. Stockman, Sharpe L.T., Fach C., 1999



Andrew Stockman

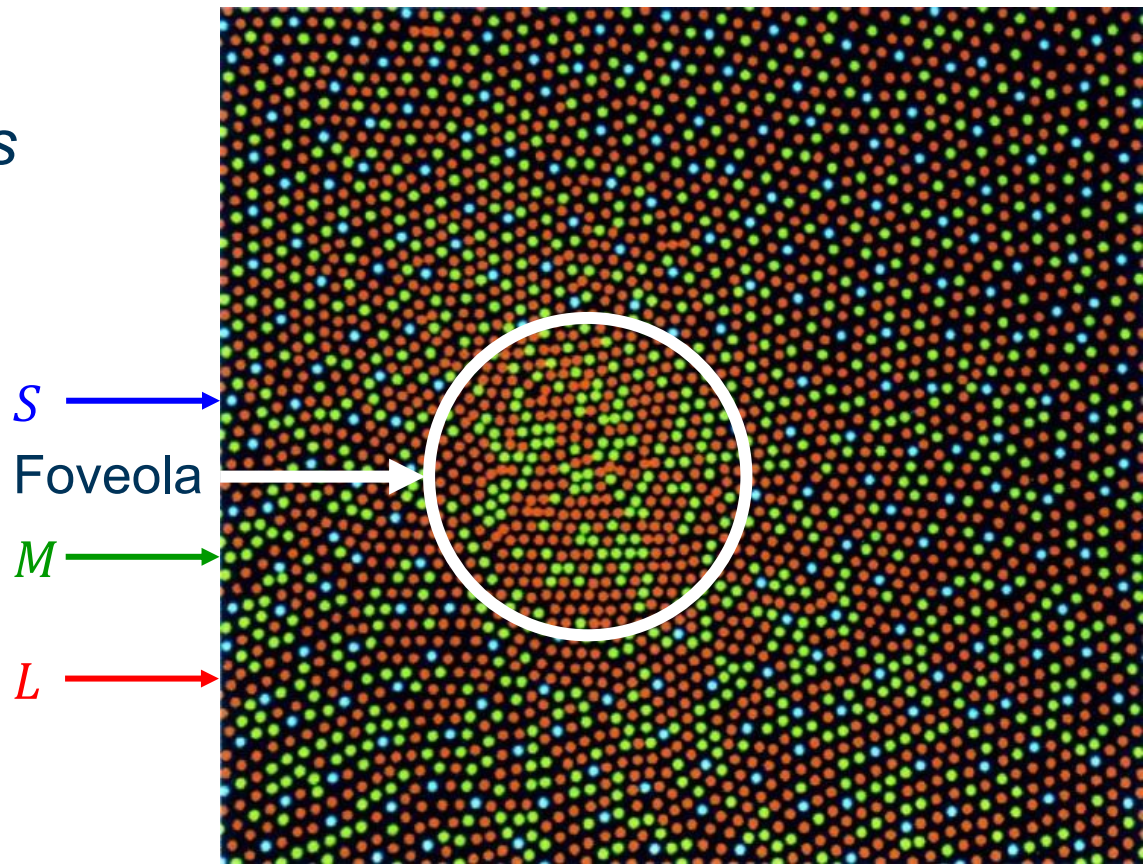
- 29 genetically controlled dichromats (D, P; 18...45 y)
- Flicker photometry 2° and 10° : 560 nm vs. λ | 25 Hz & 16 Hz
- Monochromatic background 430 nm | 680 cd/m^2 | 18°
- Cross-check with colourimetric data of 9 (2°) and 39 (10°) subj. (Stiles, Burch, 1955 and 1959).
- Cross-check with receptor absorptance spectra (Dartnall et al., 1983).



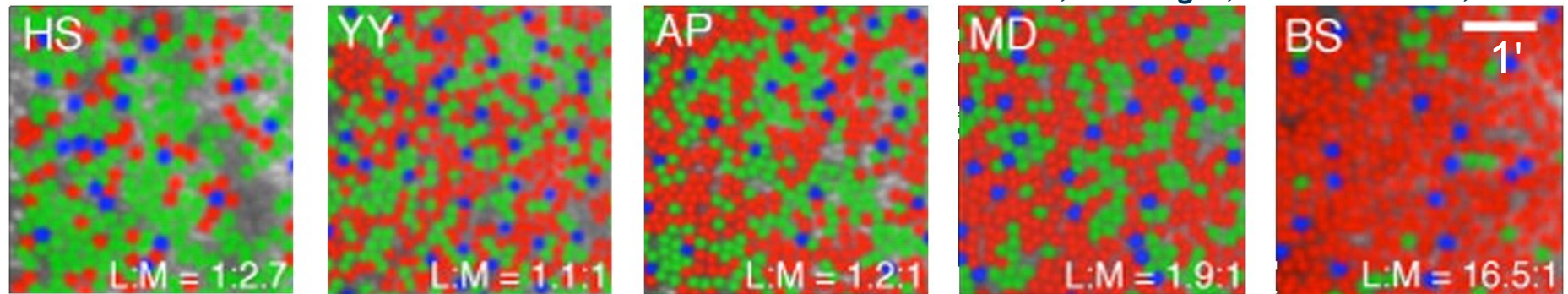
Receptor mosaic

Distribution of cone types

- Psychophysical data suggest that the relative number of receptor types in the 2° field is **1:17:34** (Vos, 1990).
- Does the number of receptor types determine the spectral luminous sensitivity?
- Apparently not: the individual absolute sensitivities of the receptor types are decisive.



Individual distributions

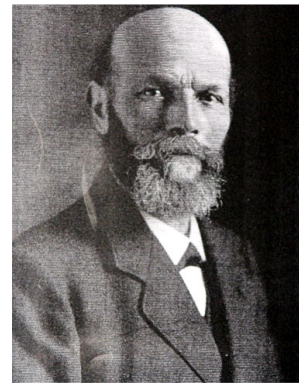


H. Hofer, B. Singer, D.R. Williams, 2005

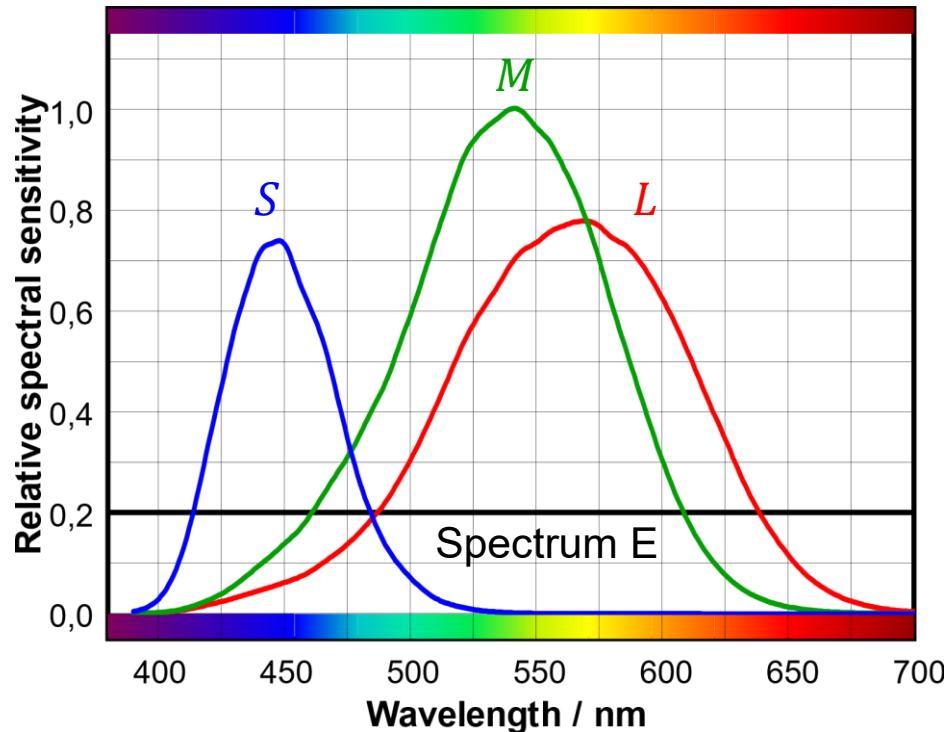
Von Kries chromatic adaptation transform

von Kries coefficients k_S , k_M , k_L

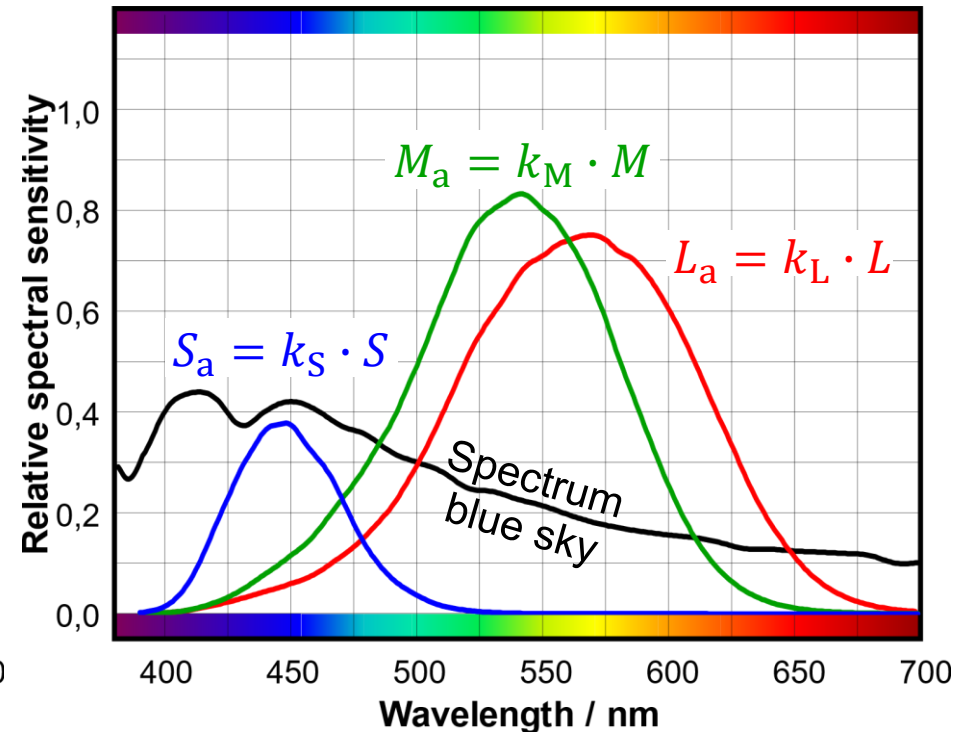
Johannes von Kries
(1853-1928)



Receptors equally strongly adapted to the equal energy spectrum E



Colour adaptation to the spectrum of the blue sky



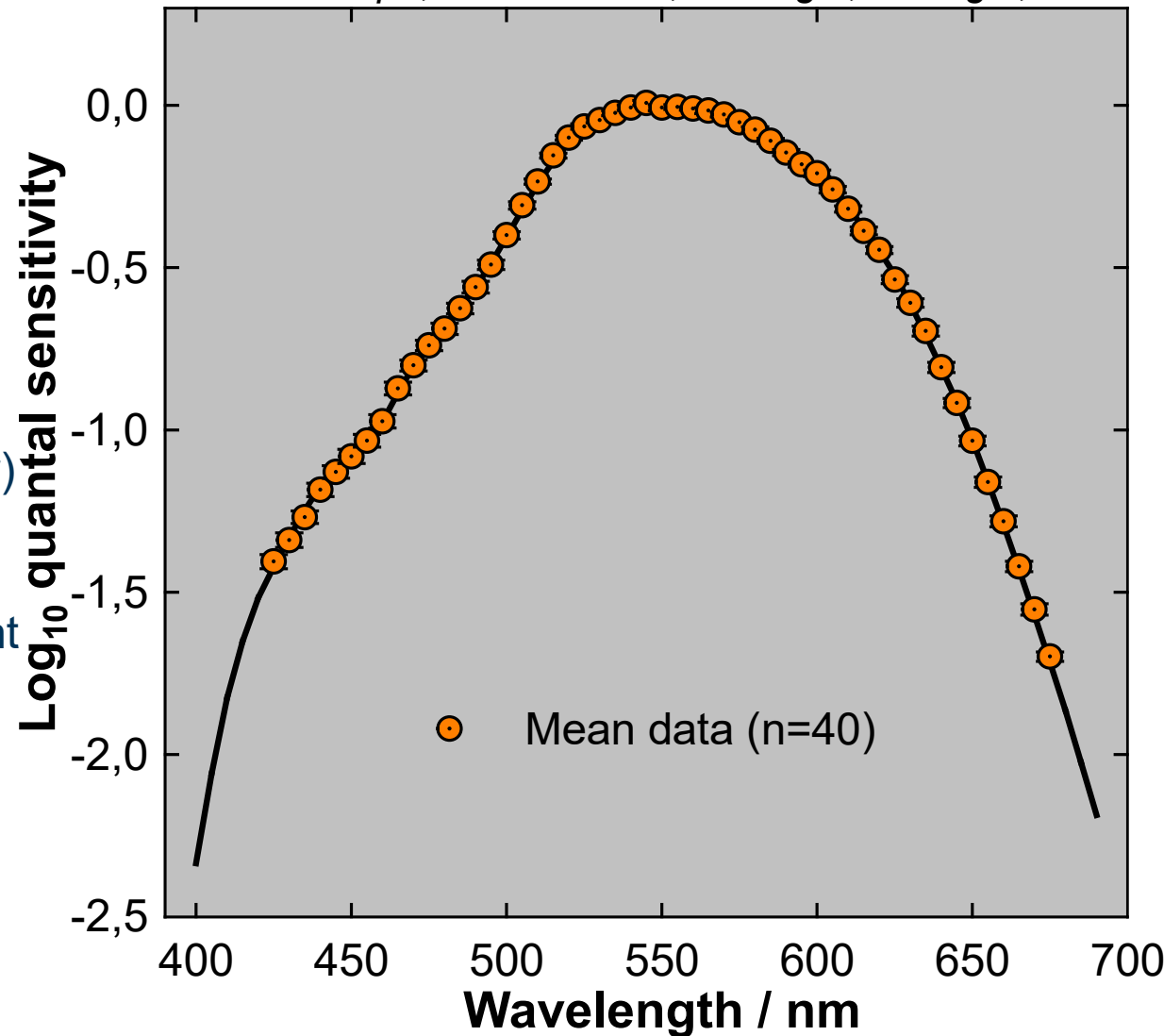
Luminous efficiency function $V^*(\lambda)$

Measurements in observers

L.T. Sharpe; A. Stockman; W. Jagla; H. Jägle, 2005
L.T. Sharpe; A. Stockman; W. Jagla; H. Jägle, 2011

Lindsay
Theodore
Sharpe

- 40 genetically controlled tri-chromats (5f, 25m; 18...48y)
- Flicker photometry:
560 nm vs. λ | 25 Hz | 2°
- White background, equivalent to D65 | 566 cd/m^2 | 16°
- Correction of the influence of the visual targets on colour adaptation
- Consistent with a linear combination of the M- and L-cone fundamentals



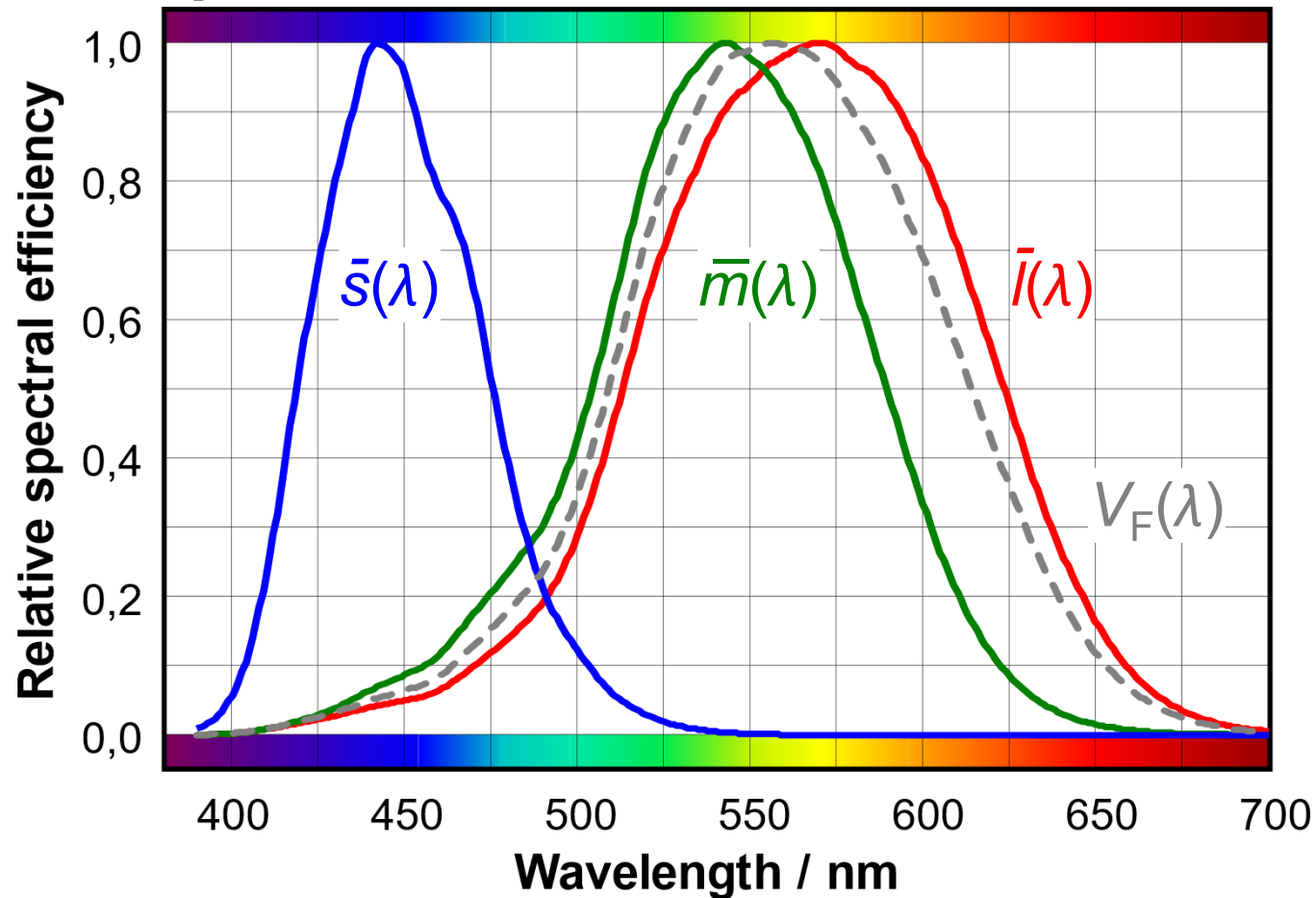
Newly proposed 2° spectral sensitivities

Cone fundamentals $\bar{l}(\lambda)$, $\bar{m}(\lambda)$, $\bar{s}(\lambda)$

Spectral luminous efficiency function $V_F(\lambda)$ for D65-adaptation

“ Grundfunktionen
basierte spektrale
Hellempfindlichkeit ”

$$V_F(\lambda) = 0,689\ 902\ 72 \cdot \bar{l}(\lambda) + 0,348\ 321\ 89 \cdot \bar{m}(\lambda)$$



L.T. Sharpe et al., 2005
CIE 170-1, 2006
L.T. Sharpe et al., 2011
CIE 170-2, 2015

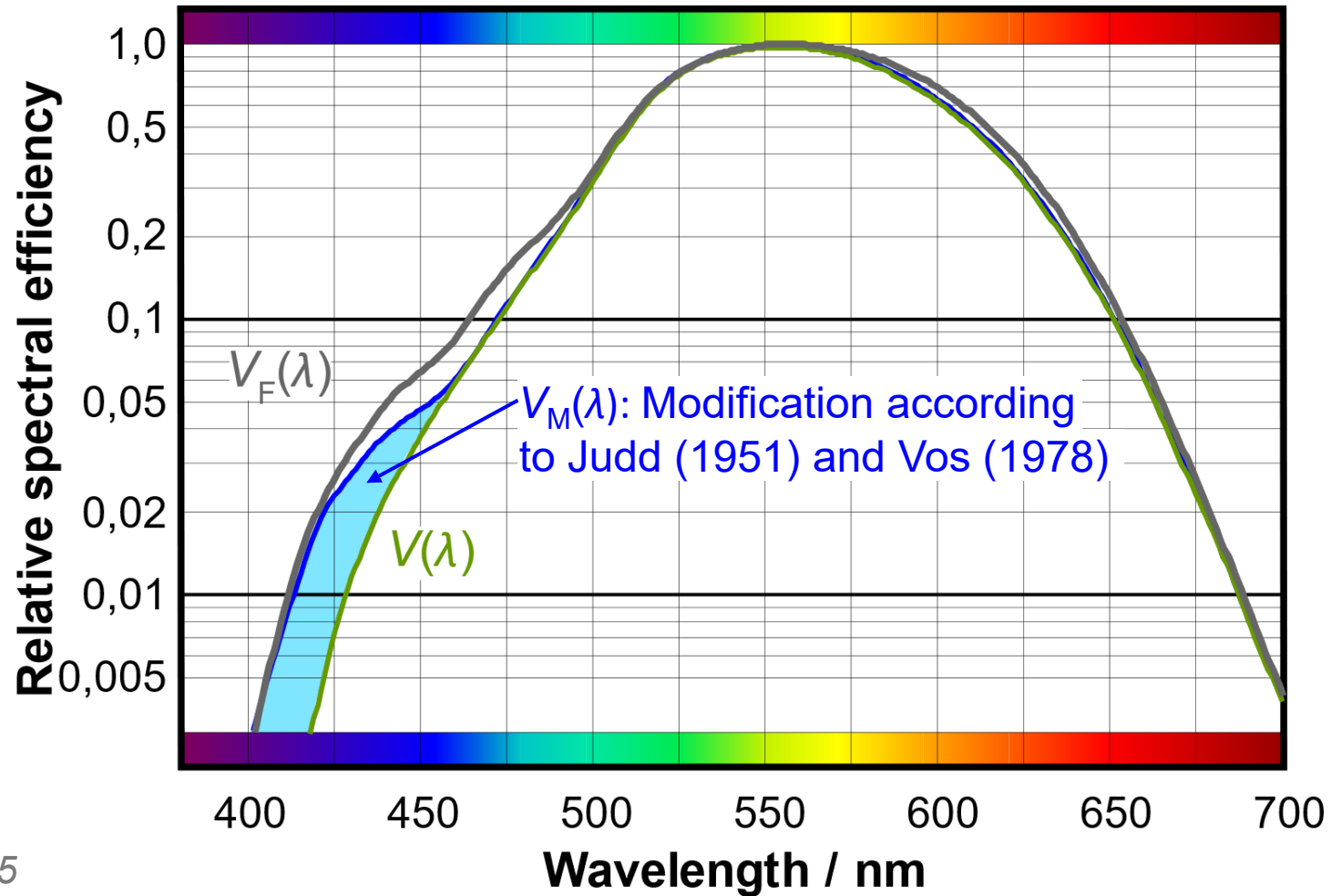
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Impact of introducing $V_F(\lambda)$

$V_M(\lambda)$: CIE 1988 Modified

$V_F(\lambda)$: Cone-Fundamental-Based

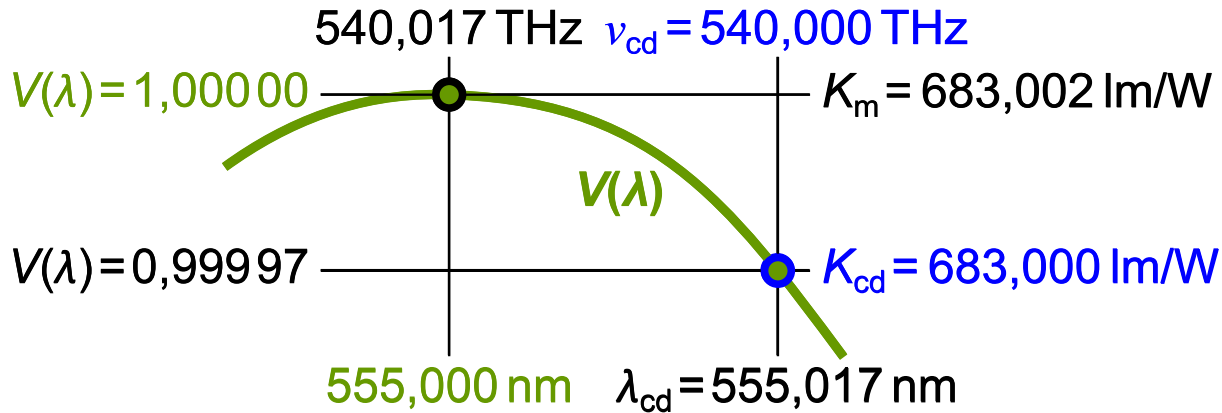


CIE Report 86:1990

CIE Report 170-2:2015

Impact of introducing $V_F(\lambda)$

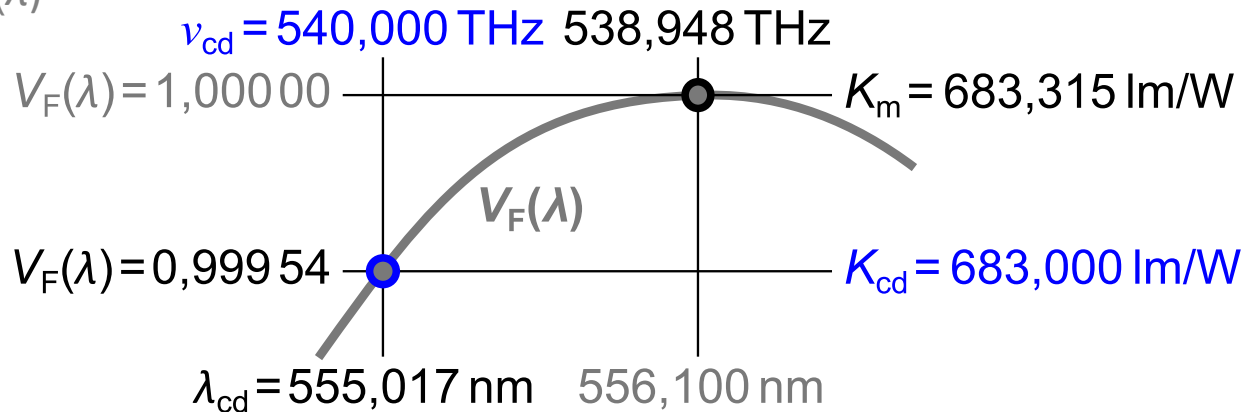
Definition of SI unit "Candela"



Anchored by definition of Candela

Anchored by definition of $V(\lambda)$

Anchored by definition of $V_F(\lambda)$

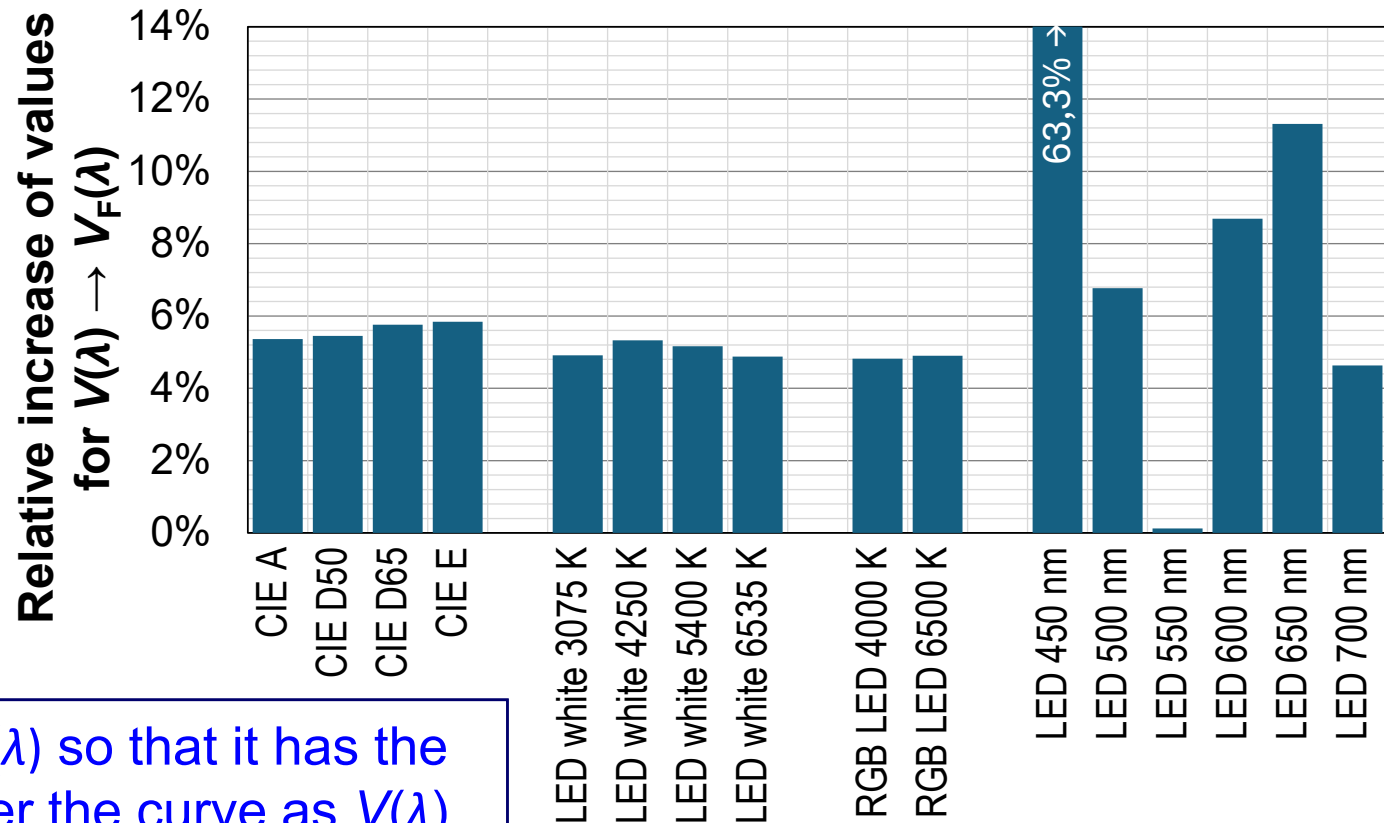


→ There is no need to change the definition of the SI unit "Candela"!

Impact of introducing $V_F(\lambda)$

Change of photometric values
for typical light sources

→ Is there nevertheless
a need to change the
definition of the
SI unit “Candela”?



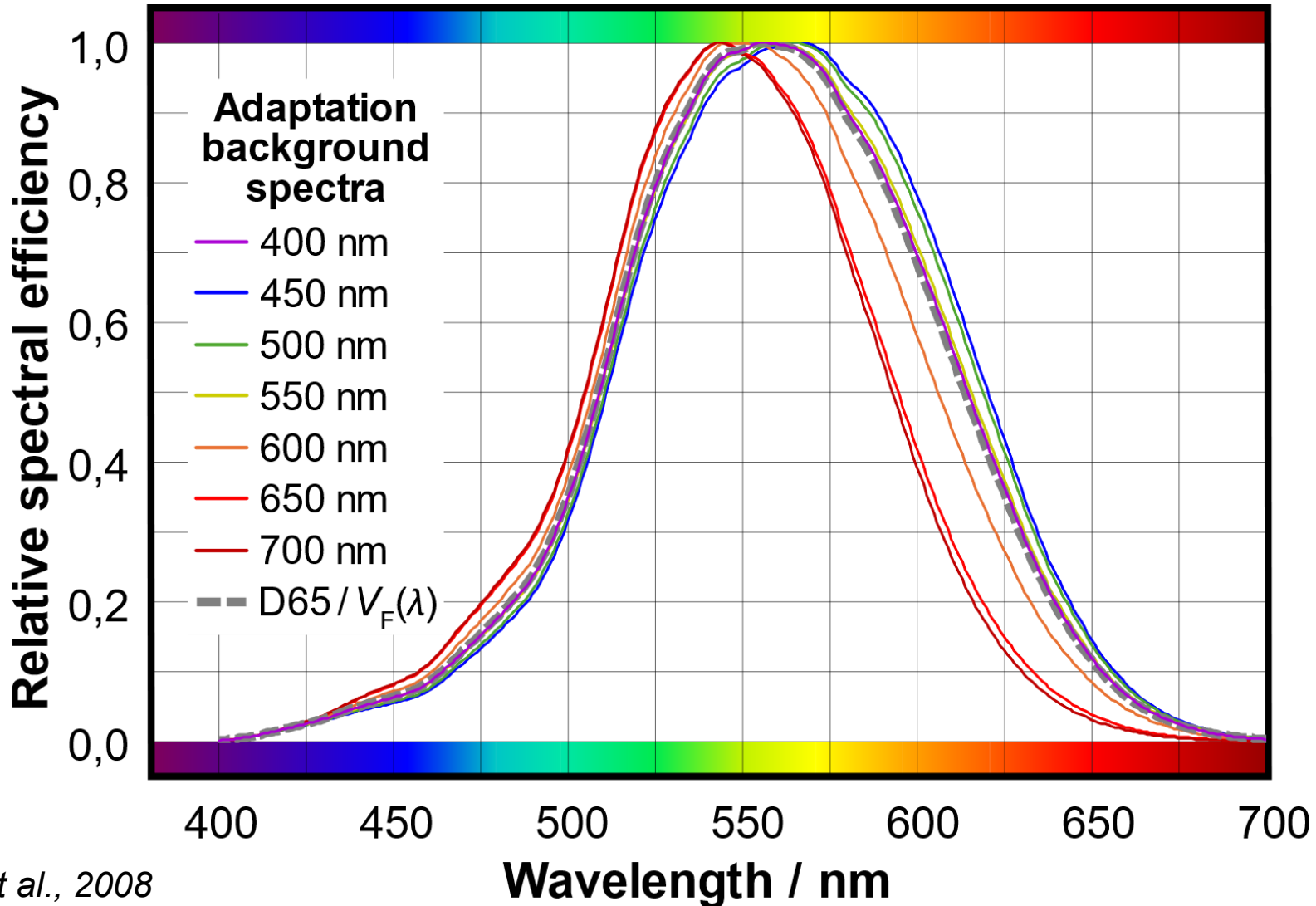
→ No! Reduce $V_F(\lambda)$ so that it has the same area under the curve as $V(\lambda)$ or use equivalent photometric quantities using correction factors.

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Luminous efficiency function $V_{\mu}^*(\lambda)$

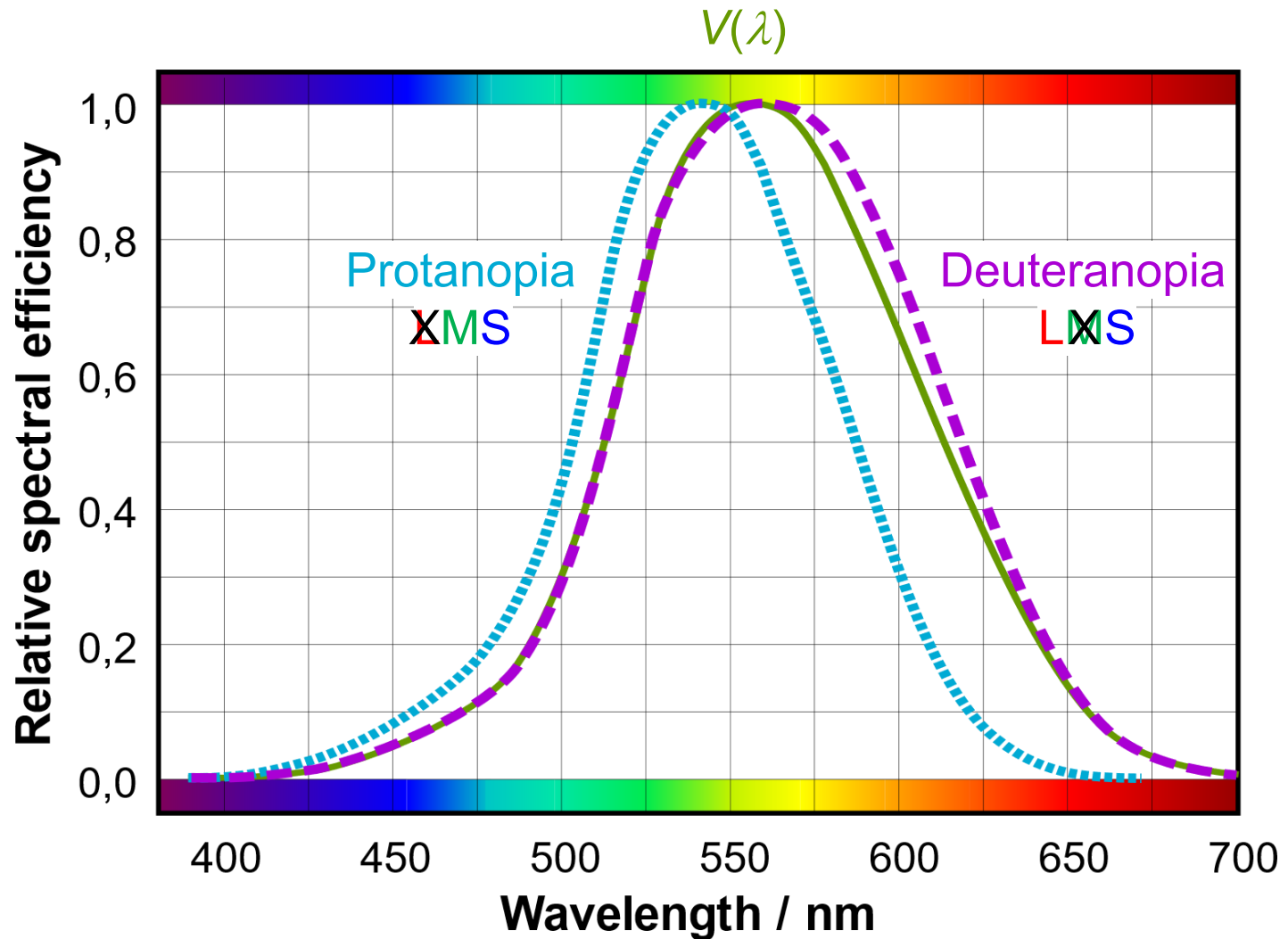
Dependence on chromatic adaptation



A. Stockman et al., 2008

Spectral luminous efficiency

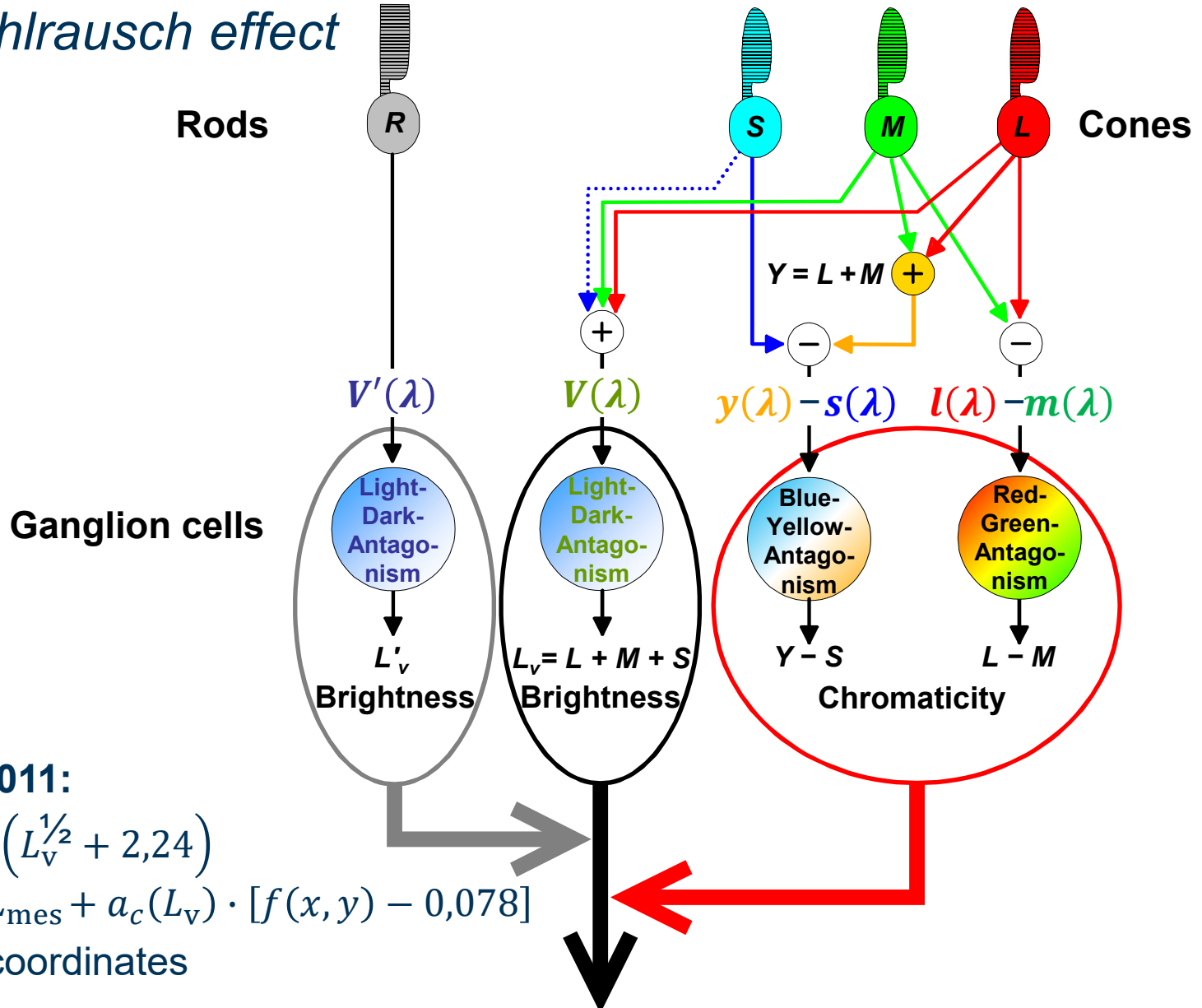
Red-green colour blindness



D.B. Judd, 1979

Influences not considered

Helmholtz-Kohlrausch effect



CIE-Report 200:2011:

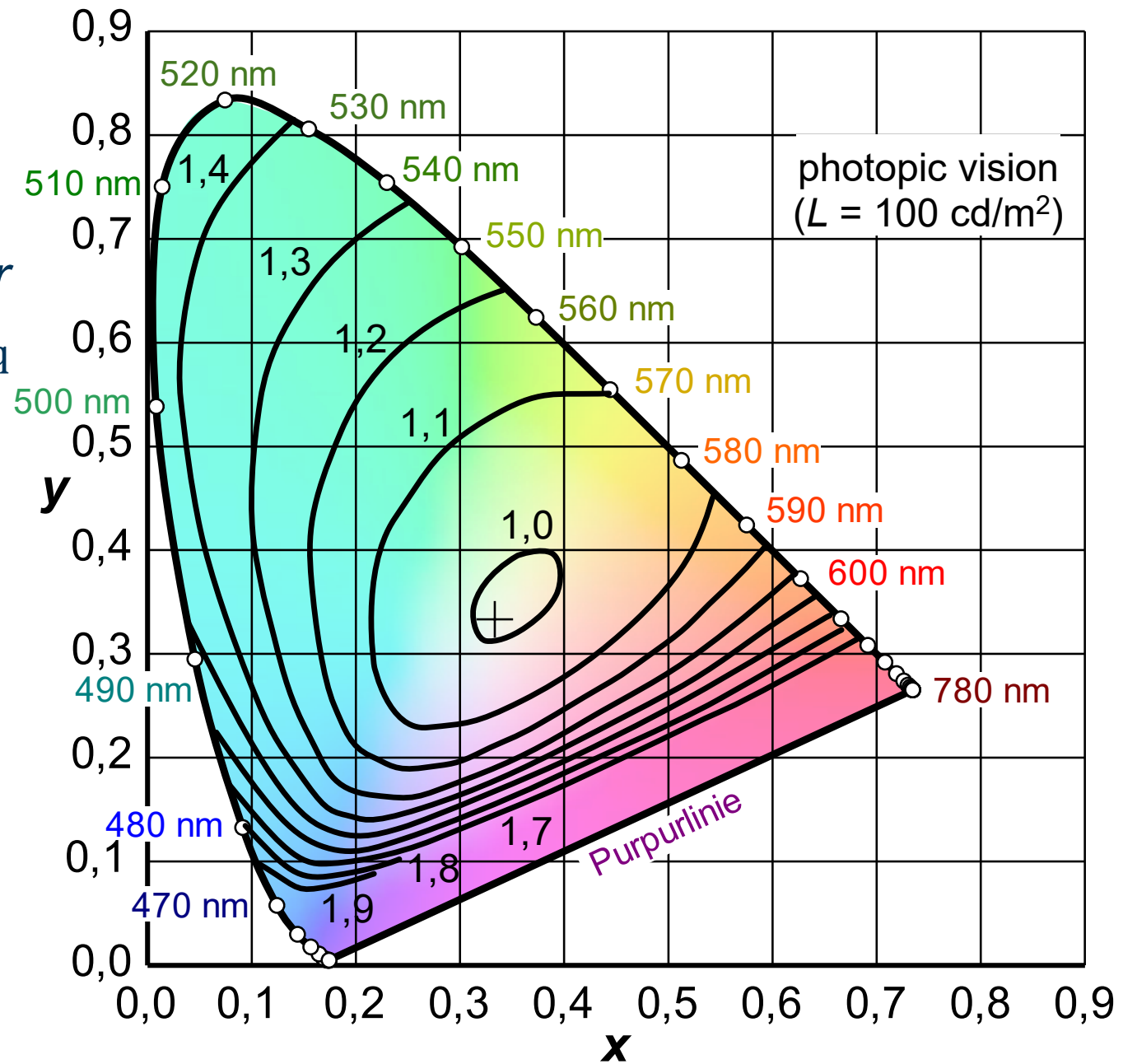
$$a_c(L_V) = 1,3 \cdot L_V^{1/2} / (L_V^{1/2} + 2,24)$$

$$\log_{10} L_{eq} = \log_{10} L_{mes} + a_c(L_V) \cdot [f(x, y) - 0,078]$$

x, y : chromaticity coordinates

Helmholtz-Kohlrausch effect

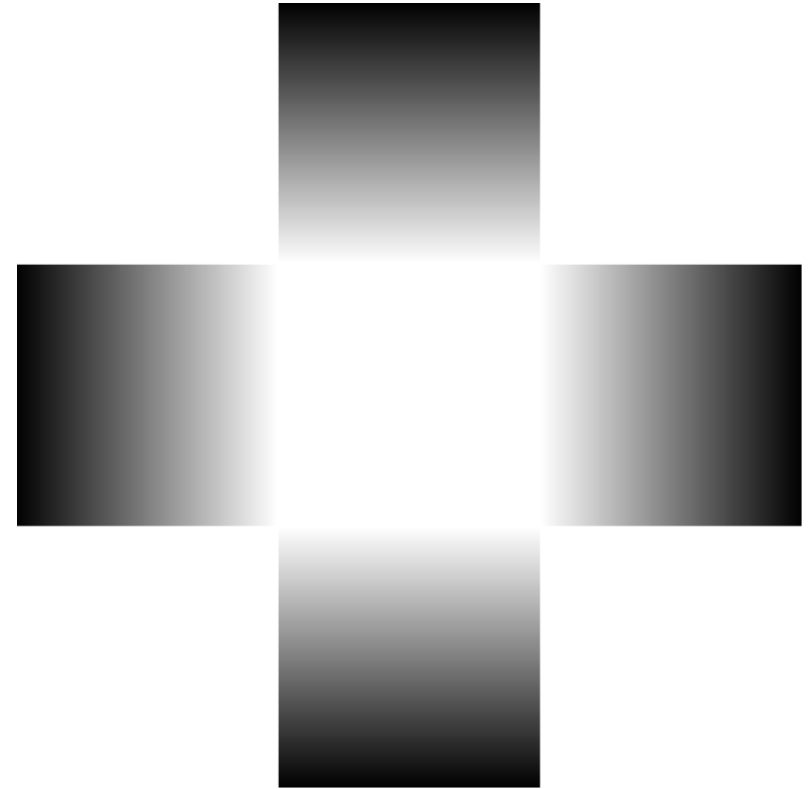
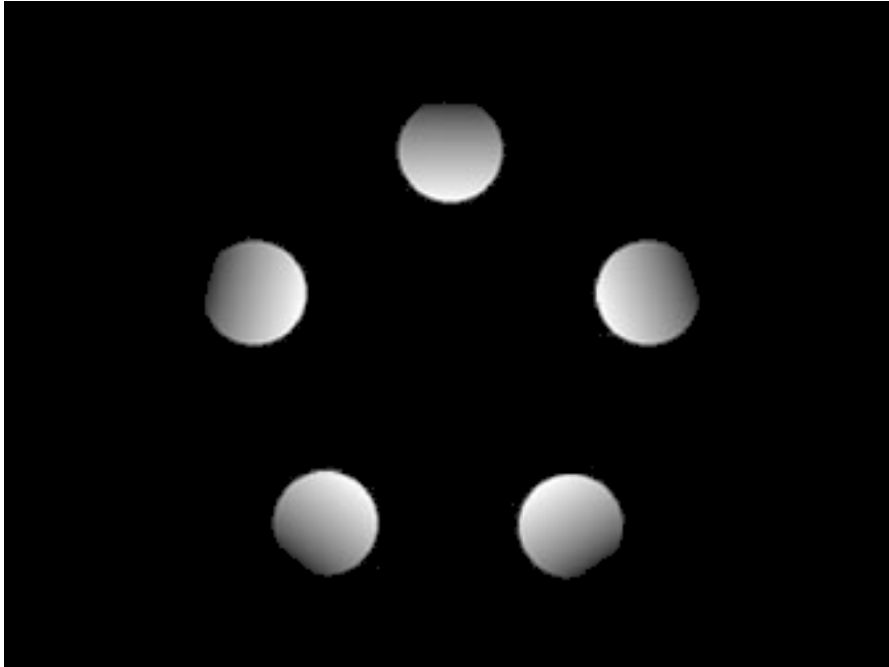
Factor $10^{f(x,y)}$ for the luminance L_{eq} equivalent to white light



K. Sagawa, 2006

Influence of context

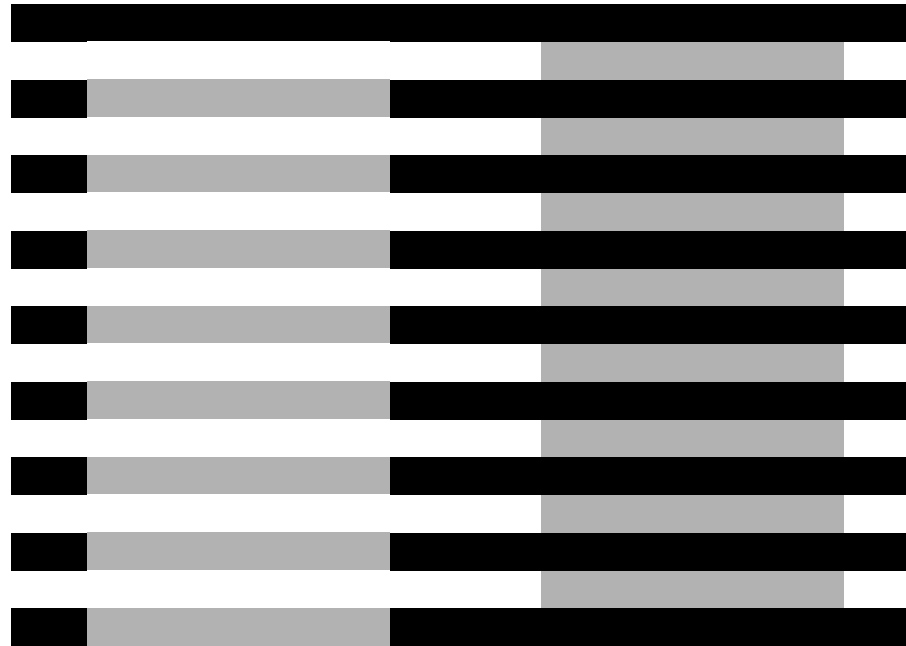
Phantom illumination illusion



Daniele Zavagno, 2005

Influence of context

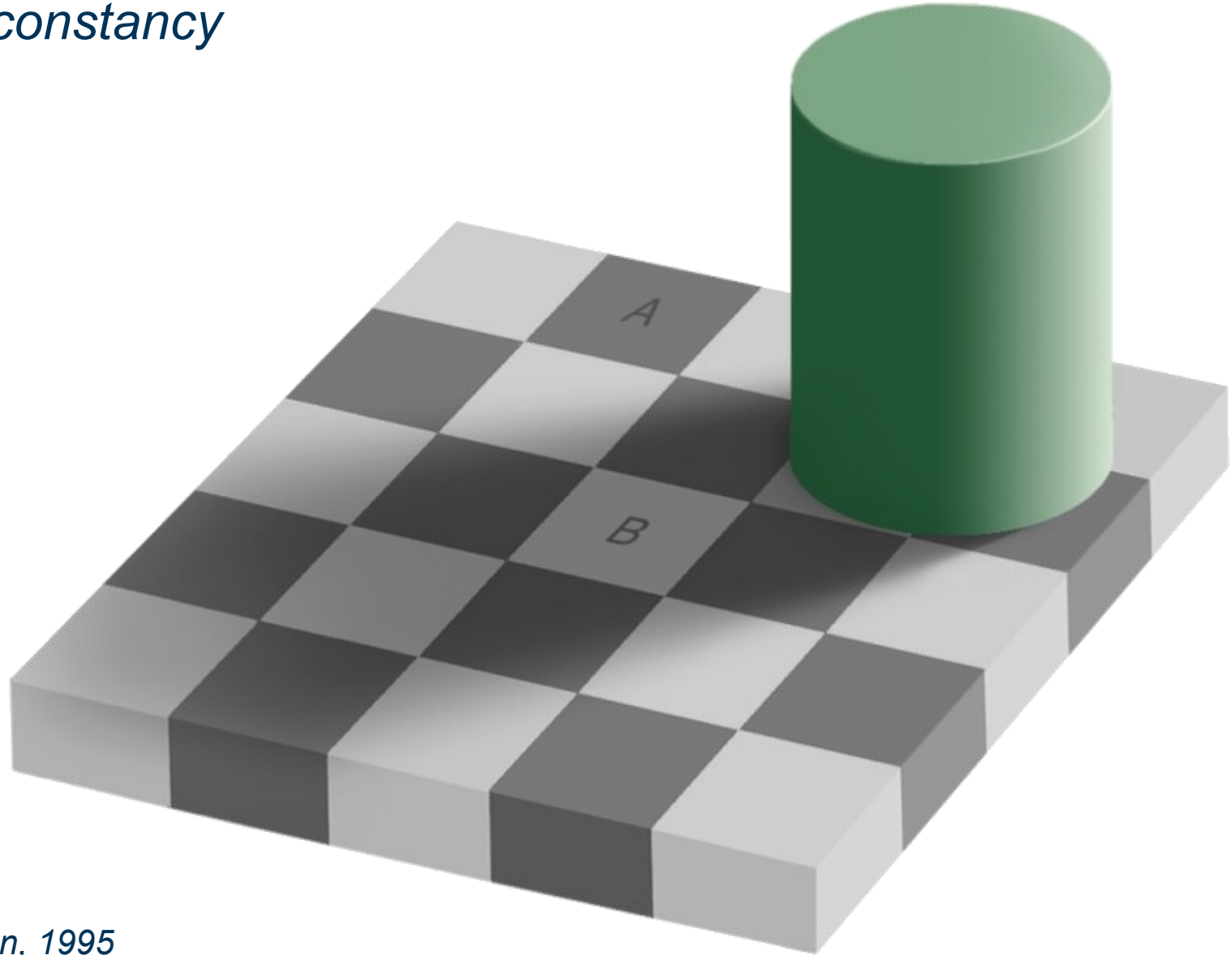
White's illusion



M. White, 1979

Influence of context

Brightness constancy



Edward H. Adelson, 1995

Summary

- Until the beginning of the 20th century, photometry was carried out visually by comparing brightness with a known reference light source.
- Visual photometry becomes inaccurate with different coloured light sources. In addition, the development of photocells at the end of the 19th century required knowledge of the spectral light sensitivity of humans.
- Studies with test subjects showed that flicker photometry and direct heterochromatic photometry using the step-by-step method provided reliable brightness sensitivity functions that also fulfil linear additivity (Abney's law).
- Based on such investigations, the CIE introduced the photopic spectral luminous efficiency function $V(\lambda)$ in 1924, which is still in use today.
- Later, the CIE introduced further $V(\lambda)$ -functions that corrected errors in the short-wave spectral range, or are suitable for scotopic and mesopic vision, for other field sizes, for different ages of persons or for monochromatic light sources.
- The latest development is a photometric (and colourimetric) system based on cone fundamentals $\bar{l}(\lambda)$, $\bar{m}(\lambda)$ and $\bar{s}(\lambda)$. A new spectral luminous efficiency function $V_F(\lambda)$, which is compatible with this for illuminant D65, has been published.
- Whether $V_F(\lambda)$ should replace or supplement the existing $V(\lambda)$ and thus jeopardise the SI-unit Candela is currently the subject of controversial debate.
- Colour adaptation to other illuminants, other field sizes and other ages are not considered. However, models for this could be developed.
- Cognitive processes of brightness perception remain unconsidered.

**Thank you for your
attention!**

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